### 8. Quadrilaterals

Q 1 Name a quadrilateral whose each pair of opposite sides is equal.

Mark (1)

Q 2 What is the sum of two consecutive angles in a parallelogram?

Mark (1)

Q 3 The angles of quadrilateral are respectively  $100^{\circ}$ ,  $30^{\circ}$ ,  $92^{\circ}$  and x. Find the value of x.

Marks (2)

Q 4 The angles of quadrilateral are in the ratio 3:5:9:13. Find all the angles of the quadrilateral.

Marks (2)

Q 5 Thee sides AB and CD of a parallelogram ABCD are

bisected at E and F. Prove that EBFD is a parallelogram.

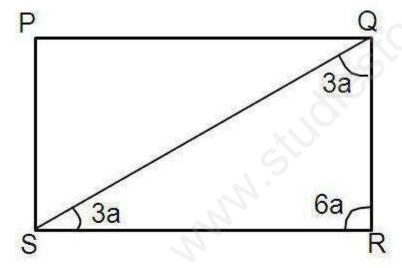
Marks (2)

Q 6 In a triangle ABC, P,Q and R are the mid – points of sides BC, CA and AB respectively.

If AC = 21 cm, BC = 29 cm and AB = 30 cm, find the perimeter of the quadrilateral ARPQ.

Marks (2)

Q 7 Find the four angles P, Q, R and S in the parallelogram PQRS as shown below.



Marks (2)

Q 8 Two opposite angles of a parallelogram are  $(5x + 1)^{\circ}$  and  $(49 - 3x)^{\circ}$ .

Find the measure of these opposite angles of the parallelogram.

Marks (2)

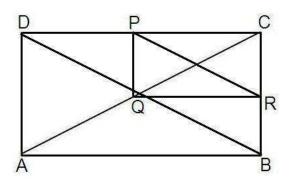
Q 9 Prove that each of the four sides of a rhombus is of the same length.

Marks (2)

Q 10 ABCD is a rhombus. Show that diagonals AC bisects angle A as well as angle C.

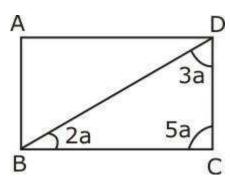
Marks (2)

Q 11 In the figure given below ,ABCD and PQRC are rectangles and Q is the mid – point of AC. Prove that  $PR = \frac{1}{2} AC$ .



Marks (2)

Q 12 Find the values of a and also find angles related to a as shown in the figure.



Marks (3)

Q 13 Prove that angle bisectors of a parallelogram form a rectangle.

Marks (3)

Q 14 ABC is an isosceles triangle with AB = AC and let D, F, E be the mid-points of BC, CA and AB respectively. Show that AD is perpendicular to EF and AD bisects EF.

Marks (3)

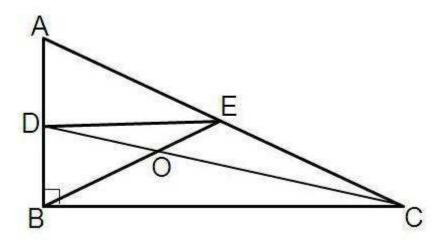
Q 15 In a triangle ABC median AD is produced to X such that AD = DX. Prove that ABXC is a parallelogram.

Marks (3)

Q 16 ABCD is parallelogram. P is a point on AD such that AP = 1/3 AD and Q is a point on BC such that CQ = 1/3 BC. Prove that AQCP is a parallelogram.

Marks (3)

Q 17 In the figure given below, triangle ABC is right – angled at B. Given that AB = 9 cm, AC = 15 cm and D, E are the mid – points of the sides AB and AC respectively, calculate the area of trapezium DECB.



Marks (3)

Q 18 ABCD is a rhombus. AD is produced to E so that DE = DC and EC produced meets AB produced in F. Prove that BF = BC.

Marks (4)

Q 19 In a quadrilateral ABCD, CO and DO are the bisectors of  $\angle$ C and  $\angle$ D respectively. Prove that

$$\angle COD = \frac{1}{2}(\angle A + \angle B)$$

Marks (4)

Q 20 AD is the median of  $\triangle$  ABC. E is the mid point of AD. BE produced meet AC at F. Show that AF=(1/3)AC.

Marks (4)

Q 21 Show that the quadrilateral formed by joining the mid point of the consecutive sides of a rectangle is a rhombus.

Marks (4)

Q 22 P is the mid-point of side AB of a parallelogram ABCD. A line through B parallel to PD meets DC at Q and AD produced at R. prove that AR = 2BC.

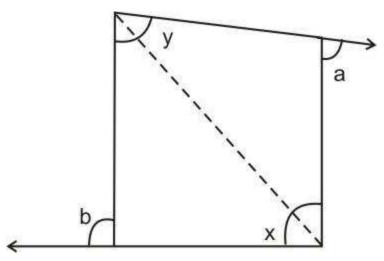
Marks (4)

Q 23 P,Q,R are, respectively, the mid points of sides AB, BC and CA and of a triangle ABC. PR and AQ meet at X. BR and PQ meet at Y. Prove that  $XY = \frac{1}{4}$  AB.

Marks (4)

#### **Most Important Questions**

- $_{Q\,1}$  The angle of a quadrilateral are respectively 100°,90°, 95°. Find the fourth angle. In a quadrilateral ABCD, the angles A,B,C and D are in the ratio 1:2:3:4.
- Find the measure of each angles of the quadrilateral.
- Q 3 The sides BA and DC of a quadrilateral ABCD are produced as shown in fig. Prove that a + b = x + y.



Q 4 The angles of a quadrilateral are in the ratio 3:5:9:13. Find all the angles of the quadrilateral.

Q 5

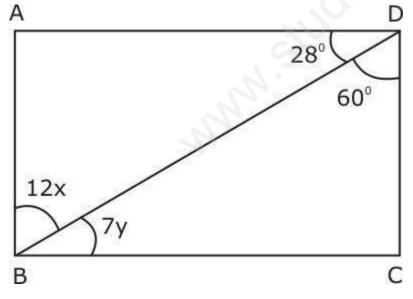
In a quadrilateral ABCD, AO and BO are the bisectors of  $\angle A$  and  $\angle B$  res Prove that  $\angle AOB = \frac{1}{2}(\angle C + \angle D)$ .

Q 6 In a parallelogram ABCD, prove that sum of any two consecutive angles is 180°.

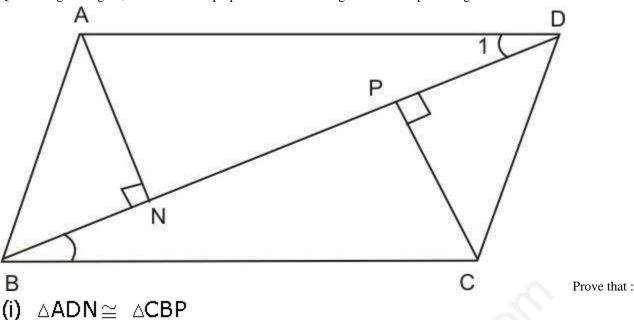
Q 7

In a parallelogram ABCD,  $\angle D = 115^{\circ}$ , determine the measure of  $\angle A$  and  $\angle B$ .

Q 8 In the given figure, ABCD is a parallelogram. Compute the values of x and y.



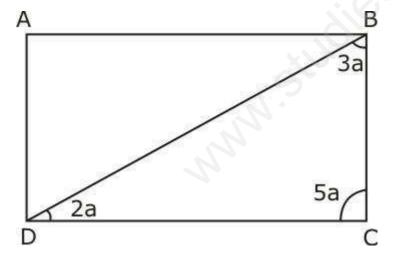
Q 9 In the given figure, AN and CP are perpendicular to the diagonal BD of a parallelogram ABCD.



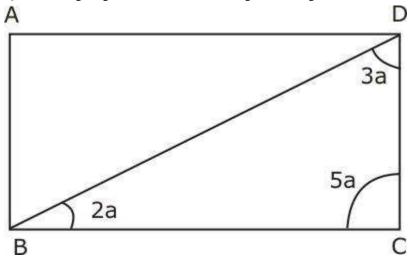
- $\triangle ADN \cong \triangle CBP$
- (ii) AN = CP

If ABCD is a quadrilateral in which AB  $\parallel$  CD and AD = BC,  $_{Q 10}$  prove that  $\angle A = \angle B$ .

Q 11 In the given figure, find the four angles A, B, C and D in the parallelogram ABCD.



Q 12 In the figure given below, find all the angles of triangle BCD.



- Q 13 Prove that angle bisectors of a parallelogram forms a rectangle.
- Q 14 AB and CD are the two parallel lines which are cut by a transversal l in point X and Y respectively. The bisectors of interior angles intersect in P and Q. form a parallelogram. Is it a rectangle?
- Q 15 ABCD is a Rhombus AD is produced to E so that DE = DC and EC produced meets AB produced in F. prove that BF = BC.
- Q 16 In a quadrilateral ABCD, CO and DO are the bisector of  $\angle$ C and  $\angle$ D respectively. Prove that  $\angle$ COD =  $(1/2)(\angle$ A +  $\angle$ B
- Q 17 ABC be an isosceles triangle with AB = AC and let D, E, F are the mid-points of BC, CA and AB respectively. Show that AD perpendicular to EF ad AD bisector of EF.
- Q 18 In triangle ABC, AD is the median through A and E is the mid-point of AD. BE produced meets AC in F proved that AF = 1/3 AC
- Q 19 Show that the quadrilateral formed by joining the mid point of the consecutive sides of a rectangle is a rhombus.
- Q 20 ABCD is parallelogram. P is a point on AD such that AP = 1/3 AD and Q is a point on BC such that CQ = 1/3 BP. Prove that AQCP is a parallelogram.
- Q 21 In a triangle ABC median AD is produced to X such that AD = DX. Prove that ABXC is a parallelogram.
- Q 22 P is the mid-point of side AB of a parallelogram ABCD. A line through B parallel to PD meets DC at Q and AD produced at R. prove that AR = 2BC.
- Q 23 P, Q, R are, respectively, the mid points of sides BC,CA and AB of a triangle ABC. PR and BQ meet at X. CR and PQ meet at Y. prove that  $XY = \frac{1}{4}$  BC