## RATIONAL NUMBERS

A number which can be written as $\frac{p}{q}$, where $p$, $q$, are integers and $q^{1} 0$, is called a rational number Thus, an integer divided by a non-zero integer is called rational number.
Ex. $\frac{2}{3}, \frac{37}{15}, \frac{-17}{19},-3,0,10,4.33,7.123123123 \ldots \ldots \ldots$
In rational number $\frac{\mathrm{p}}{\mathrm{q}}$, p is called first integer or numerator and q the second integer or denominator.
(I) Positive rational numbers: A rational number is said to be positive, if its numerator and denominator are either both positive or both negative

Ex. $\frac{5}{7}$ and $\frac{-2}{-3}$ are both positive rational numbers.
(II) Negative rational numbers: A rational number is said to be negative, if its numerator and denominator are of opposite sign $\frac{-4}{9}$ and $\frac{5}{-12}$ are negative rational numbers,
(III) Equivalent rational numbers: If $\frac{\mathrm{a}}{\mathrm{b}}$ is a rational number and m is a nonzero integer then $\frac{\mathrm{a}}{\mathrm{b}}=\frac{\mathrm{a} \times \mathrm{m}}{\mathrm{b} \times \mathrm{m}}$

Ex. $\quad-\frac{3}{4}=\frac{-3 \times 2}{4 \times 2}=\frac{-3 \times 3}{4 \times 3}=\ldots$.
$-\frac{3}{4}=\frac{-6}{8}=\frac{-9}{12}=\ldots$. Such rational number are called equivalent rational numbers.

(a) Natural Numbers (N): The counting numbers 1, 2, 3, .... are known as natural numbers. $\mathrm{N}=(1,2,3,4, \ldots$.

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(b) Whole Numbers (W) : The number '0' together with the natural numbers 1, 2, 3, ... are known as whole numbers.

(c) Integers (I or $\mathbf{Z}) \quad:$ All natural numbers, 0 and negative of natural numbers are called integers. $I=\{-¥, \ldots . .-3,-2,-1,0,1,2,3 \ldots . \neq\}$
Positive integers : $(1,2,3,4, \ldots .$.$) ; Negative integers : (\ldots-4,-3,-2,-1)$

(v) The set of non-positive integer $=\{\ldots \ldots-4,-3,-2,-1,0\}$

## NATURAL NUMBERS, WHOLE NUMBERS, INTEGERS AND FRACTION AS RATIONAL NUMBERS

(i) Since a natural number $\mathrm{n}=\frac{\mathrm{n}}{1}=\frac{\text { an integer }}{\text { a non - zero integer }}$ every natural number is a rational number.
(ii) Now, $0=\frac{0}{\text { any non - zero integer }}$, and is therefore a rational number.

P All natural numbers and 0 being rational numbers imply,
all whole numbers are rational numbers.
(iii) Any integer $(\ldots-3,-2,-1,0,1,2,3, \ldots .$.$) can be written as \frac{p}{q}$. where p is the given integer and $\mathrm{q}=1$ is the non-zero integer.

Thus, every integer is a rational number.
(iv) A fraction $=\frac{x}{y}$, where $x$ and $y$ are natural numbers i.e., positive integer.

Thus, every fraction $=\frac{\text { an integer }}{a \text { non zero integer }}$ and is a rational number.
(i) Every natural number, whole number and integer is a rational number.
(ii) Every terminating decimal is a rational number.
(iii) Every non-terminating repeating (recurring) decimal is a rational number.
(iv) Between any two rational numbers there are an infinite number of rational numbers.

This property is known as the density of rational numbers.

## PROPERTIES OF RATIONAL NUMBERS

(I) If $\frac{\mathrm{a}}{\mathrm{b}}$ and $\frac{\mathrm{c}}{\mathrm{d}}$ are two rational numbers then $\frac{\mathrm{a}}{\mathrm{b}}+\frac{\mathrm{c}}{\mathrm{d}}=\frac{\mathrm{ad}+\mathrm{bc}}{\mathrm{bd}}$
(II) If $\frac{\mathrm{a}}{\mathrm{b}}$ and $\frac{\mathrm{c}}{\mathrm{d}}$ are two rational numbers then $\frac{\mathrm{a}}{\mathrm{b}} \times \frac{\mathrm{c}}{\mathrm{d}}=\frac{\mathrm{a} \times \mathrm{c}}{\mathrm{b} \times \mathrm{d}}$
(III) If $\frac{\mathrm{a}}{\mathrm{b}}$ and $\frac{\mathrm{c}}{\mathrm{d}}\left({ }^{1} 0\right)$ are two rational numbers, then $\frac{\mathrm{a}}{\mathrm{b}}, \frac{\mathrm{c}}{\mathrm{d}}=\frac{\mathrm{a}}{\mathrm{b}} \times \frac{\mathrm{d}}{\mathrm{c}}=\frac{\mathrm{ad}}{\mathrm{bc}}$
(IV) if $\frac{a}{b}, \frac{c}{d}$ and $\frac{e}{f}$ are three rational numbers then $\frac{a}{b} \times\left(\frac{c}{d}+\frac{e}{f}\right)=\left(\frac{a}{b} \times \frac{c}{d}\right)+\left(\frac{a}{b} \times \frac{e}{f}\right)$ and $\frac{\mathrm{a}}{\mathrm{b}} \times\left(\frac{\mathrm{c}}{\mathrm{d}}-\frac{\mathrm{e}}{\mathrm{f}}\right)=\left(\frac{\mathrm{a}}{\mathrm{b}} \times \frac{\mathrm{c}}{\mathrm{d}}\right)-\left(\frac{\mathrm{a}}{\mathrm{b}} \times \frac{\mathrm{e}}{\mathrm{f}}\right)$ (Distributive property of multiplication over addition and subtraction)
(V) If $\frac{\mathrm{a}}{\mathrm{b}}$ and $\frac{\mathrm{c}}{\mathrm{d}}$ be two rational number then $\frac{\mathrm{a}}{\mathrm{b}}=\frac{\mathrm{c}}{\mathrm{d}} \mathrm{p}$ a $\times \mathrm{d}=\mathrm{b} \times \mathrm{c}$
(VI) Absolute value of a rational number


## RECIPROCAL OR MULTIPLICATIVE INVERSE AND ADDITIVE INVERSE

(i) Reciprocal : Every non-zero rational number $\frac{\mathrm{a}}{\mathrm{b}}$ has its multiplicative inverse $\frac{\mathrm{b}}{\mathrm{a}}$

Thus $\left(\frac{a}{b} \times \frac{b}{a}\right)=\left(\frac{b}{a} \times \frac{a}{b}\right)=1 \triangleright \frac{b}{a}$ is called the reciprocal of $\frac{a}{b}$
(ii) Multiplicative inverse : We denote the reciprocal of $\frac{a}{b}$ by $\left(\frac{a}{b}\right)^{-1}$ Clearly $\left(\frac{a}{b}\right)^{-1}=\frac{b}{a}$
(iii) Additive Inverse : For every rational number $\frac{\mathrm{a}}{\mathrm{b}}$, there exists a rational number $\frac{-\mathrm{a}}{\mathrm{b}}$
such that $\quad\left(\frac{a}{b}+\frac{-\mathbf{a}}{\mathbf{b}}\right)=\frac{\mathbf{a}+(-\mathbf{a})}{\mathbf{b}}=\frac{\mathbf{0}}{\mathbf{b}}=0$ and $\left(-\frac{\mathbf{a}}{\mathbf{b}}+\frac{\mathbf{a}}{\mathbf{b}}\right)=0$

$$
-\frac{\mathbf{a}}{\mathbf{b}} \text { is called the additive inverse of } \frac{a}{b}
$$

Ex. $\quad\left(\frac{4}{7}+\frac{-4}{7}\right)=\frac{\{4+(-4)\}}{7}=\frac{0}{7}=0$ and similarly, $\left(\frac{-4}{7}+\frac{4}{7}\right)=0$
1 $\left(\frac{4}{7}+\frac{-4}{7}\right)=\left(\frac{-4}{7}+\frac{4}{7}\right)=0$
Thus, $\frac{4}{7}$ and $\frac{-4}{7}$ are additive inverses of each other.
Ex. Find the Reciprocal of -3 and $\frac{-8}{9}$, since

$$
\left(-3 \times \frac{-1}{3}\right)=\left(\frac{-3}{1} \times \frac{-1}{3}\right)=\frac{(-3) \times(-1)}{1 \times 3}=\frac{3}{3}=1
$$

and Reciprocal of $\frac{-8}{9}$ is $\frac{-9}{8}$, since $\left(\frac{-8}{9} \times \frac{-9}{8}\right)=\left(\frac{-9}{8} \times \frac{-8}{9}\right)=1$
Ex. Find the additive inverse of :
(a) $\frac{5}{9}$
(b) $\frac{-15}{8}$
(c) $\frac{-6}{-7}$

Sol. (a) Additive inverse of $\frac{5}{9}$ is $\frac{-5}{9}$
(b) Additive inverse of $\frac{-15}{8}$ is $\frac{15}{8}$
(c) We may write, $\frac{-6}{-7}=\frac{(-7) \times(-1)}{(-7)}=\frac{6}{7}$. Hence, its additive inverse is $\frac{-6}{7}$

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Write the additive inverse of (a) $\frac{-10}{31}$
(b) $\frac{4}{-15}$
(c) $\frac{-2}{-7}$
(d) $\frac{15}{9}$

Find the reciprocal of each of the following : (a) 12 (b) -8
$\begin{array}{ll}\text { (c) } \frac{5}{16} & \text { (d) } \frac{-14}{17}\end{array}$
(e) $\frac{0}{2}$

## ADDITIVE IDENTITY AND MULTIPLICATIVE IDENTITY

(i) Additive identity : 0 is a rational number such that the sum of any rational number and 0 is the rational number it self.

Thus $\left(\frac{\mathbf{a}}{\mathbf{b}}+\mathbf{0}\right)=\left(\mathbf{0}+\frac{\mathbf{a}}{\mathbf{b}}\right)=\frac{\mathbf{a}}{\mathbf{b}}$, for every rational number $\frac{\mathrm{a}}{\mathrm{b}}$
$\mathbf{0}$ is called the additive identity for rationals.
(ii) Multiplicative Identity : For any rational number $\frac{a}{b}$, we have $\left(\frac{a}{b} \times 1\right)=\left(1 \times \frac{a}{b}\right)=\frac{a}{b}$

1 is called the multiplicative identity for rationals.

Ex. (i) $\left(\frac{3}{5}+0\right)=\left(\frac{3}{5}+\frac{0}{5}\right)=\frac{3}{5}$ and similarly, $\left(0+\frac{3}{5}\right)=\frac{3}{5}$

$$
\backslash \quad\left(\frac{3}{5}+0\right)=\left(0+\frac{3}{5}\right)=\frac{3}{5}
$$

(ii) $\left(\frac{-2}{3}+0\right)=\left(\frac{-2}{3}+\frac{0}{3}\right)=\frac{(-2+0)}{3}=\frac{-2}{3}$ and similarly, $\left(0+\frac{-2}{3}\right)=\frac{-2}{3}$
$\ \quad\left(\frac{-2}{3}+0\right)=\left(0+\frac{-2}{3}\right)=\frac{-2}{3}$
Ex. (i) Consider the rational number $\frac{3}{4}$. Then, we have

$$
\begin{aligned}
& \left(\frac{3}{4} \times 1\right)=\left(\frac{3}{4} \times \frac{1}{1}\right)=\frac{(3 \times 1)}{(4 \times 1)}=\frac{3}{4} \text { and }\left(1 \times \frac{3}{4}\right)=\left(\frac{1}{1} \times \frac{3}{4}\right)=\frac{(1 \times 3)}{(1 \times 4)}=\frac{3}{4} . \\
& \\
& \left(\frac{3}{4} \times 1\right)=\left(1 \times \frac{3}{4}\right)=\frac{3}{4}
\end{aligned}
$$

(ii) Consider the rational number $\frac{-9}{13}$. Then, we have

$$
\frac{-9}{13} \times 1=\left(\frac{-9}{13} \times \frac{1}{1}\right)=\frac{(-9) \times 1}{13 \times 1}=\frac{-9}{13} . \quad \text { and }\left(1 \times \frac{-9}{13}\right)=\left(\frac{1}{1} \times \frac{-9}{13}\right)=\frac{(1) \times(-9)}{1 \times 13}=\frac{-9}{13}
$$



PROPERTIES OF ADDITION, SUBTRACTION, MULTIPLICATION \& DIVISION OF RATIONAL NUMBER

| Properties | Addition | Subtraction | Multiplicatio n | Divis io n |
| :---: | :---: | :---: | :---: | :---: |
| Closure property | $(x+y)$ is always <br> a rationalnumber | $(x-y)$ is always <br> a rationalnumber | $x \times y$ is always <br> a rationalnumber | $x \div y$ and $y \neq 0$ <br> then is always a <br> rationalnumber |
| Commutative <br> property | $x+y=y+x$ | $(x-y) \neq(y-x)$ | $x \times y=y \times x$ | $x \div y \neq y \div x$ |
| Associative property | $x+(y+z)=(x+y)+z$ | $x-(y-z) \neq(x-y)-z$ | $x \times(y \times z)=(x \times y) \times z$ | $x \div(y \div z) \neq(x \div y) \div z$ |

Note : $x, y \& z$ are rational numbers.
(-) ADDITION OF RATIONAL NUMBERS: We define $\left(\frac{a}{b}+\frac{c}{b}\right)=\frac{a+c}{b}$
Ex. Find the sum :
(i) $\frac{7}{9}+\frac{-11}{9}$
(ii) $\frac{8}{-11}+\frac{3}{11}$

Sol. Wehave

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(i) $\frac{7}{9}+\frac{-11}{9}=\frac{7+(-11)}{9}=\frac{-4}{9}$.
(ii) $\frac{8}{-11}=\frac{8 \times(-1)}{(-11) \times(-1)}=\frac{-8}{11}$.


## PROPERTIES OF ADDITION OF RATIONAL NUMBERS

(a) (Closure property ) : The sum of two rational numbers is always a rational number. If $\frac{\mathrm{a}}{\mathrm{b}}$ and $\frac{\mathrm{c}}{\mathrm{d}}$ are any two rational numbers, then $\left(\frac{\mathbf{a}}{\mathbf{b}}+\frac{\mathbf{c}}{\mathbf{d}}\right)$ is also a rational number.
Ex. Consider the rational number $\frac{1}{3}$ and $\frac{3}{4}$. Then
Sol. $\left(\frac{1}{3}+\frac{3}{4}\right)=\left(\frac{4+9}{12}\right)=\frac{13}{12}$, which is a rational number.
Ex. Consider the rational number $\frac{-2}{3}$ and $\frac{4}{5}$. Then,
Sol. $\left(\frac{-2}{3}+\frac{4}{5}\right)=\frac{(-10+12)}{15}=\frac{2}{15}$, which is a rational number.
(b) (Commutative law) : Two rational numbers can be added in any order. Thus for any two rational numbers $\frac{\mathrm{a}}{\mathrm{b}}$ and $\frac{\mathrm{c}}{\mathrm{d}}$, we have $\left(\frac{\mathrm{a}}{\mathrm{b}}+\frac{\mathbf{c}}{\mathrm{d}}\right)=\left(\frac{\mathbf{c}}{\mathrm{d}}+\frac{\mathrm{a}}{\mathrm{b}}\right)$

Ex. (i) $\left(\frac{1}{2}+\frac{3}{4}\right)=\frac{(2+3)}{4}=\frac{5}{4}$ and $\left(\frac{3}{4}+\frac{1}{2}\right)=\frac{(3+2)}{4}=\frac{5}{4}$
\ $\left(\frac{1}{2}+\frac{3}{4}\right)=\left(\frac{3}{4}+\frac{1}{2}\right)$.
(ii) $\frac{-1}{2}+\frac{-2}{3}=\frac{(-3)+(-4)}{6}=\frac{-7}{6}$ and $\left(\frac{-2}{3}+\frac{-1}{2}\right)=\left\{\frac{\{(-4)+(-3))}{6}\right\}=\frac{-7}{6}$

। $\left(\frac{-1}{2}+\frac{-2}{3}\right)=\left(\frac{-2}{3}+\frac{-1}{2}\right)$ P LHS $=$ RHS
(c) (Associative law) : While adding three rational numbers, they can be grouped in any order. thus for any three rational number $\frac{a}{b}, \frac{c}{d}$ and $\frac{e}{f}$ we have $\left(\frac{a}{b}+\frac{\mathbf{c}}{d}\right)+\frac{e}{f}=\frac{a}{b}+\left(\frac{\mathbf{c}}{\mathbf{d}}+\frac{\mathbf{e}}{f}\right)$

Ex. Consider three rational numbers $\frac{-2}{3}, \frac{5}{7}$ and $\frac{1}{6}$ then,
Sol. $\left\{\left(\frac{-2}{3}+\frac{5}{7}\right)+\frac{1}{6}\right\}=\left\{\frac{(-14+15)}{21}+\frac{1}{6}\right\}=\left(\frac{1}{21}+\frac{1}{6}\right)=\frac{(2+7)}{42}=\frac{9}{42}=\frac{3}{14}$
and $\left\{\frac{-2}{3}+\left(\frac{5}{7}+\frac{1}{6}\right)\right\}=\left[\frac{-2}{3}+\frac{(30+7)}{42}\right]=\left[\frac{-2}{3}+\frac{37}{42}\right]=\frac{(-28+37)}{42}=\frac{9}{42}=\frac{3}{14}$

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I $\left\{\left(\frac{-2}{3}+\frac{5}{7}\right)+\frac{1}{6}\right\}=\left\{\frac{-2}{5}+\left(\frac{5}{7}+\frac{1}{6}\right)\right\}$ D LHS $=$ RHS
(-) SUBTRACTION OF RATIONAL NUMBERS :
For rational numbers $\frac{a}{b}$ and $\frac{c}{d}$, we define $\left(\frac{a}{b}-\frac{\mathbf{c}}{\mathbf{d}}\right)=\frac{\mathbf{a}}{\mathbf{b}}+\left(\frac{-\mathbf{c}}{\mathbf{d}}\right)=\frac{\mathbf{a}}{\mathbf{b}}+\left(\right.$ additive inverse of $\left.\frac{\mathbf{c}}{\mathbf{d}}\right)$
Ex. (i) Subtract $\frac{3}{4}$ from $\frac{2}{3}$ (ii) Subtract $\frac{-5}{7}$ from $\frac{-2}{5}$
Sol. (i) $\left(\frac{2}{3}-\frac{3}{4}\right)=\frac{2}{3}+\left(\right.$ additive inverse of $\left.\frac{3}{4}\right)=\left(\frac{2}{3}+\frac{-3}{4}\right)=\frac{\{8+(-9)\}}{12}=\frac{-1}{12}$
(ii) $\left\{\frac{-2}{5}-\left(\frac{-5}{7}\right)\right\}=\frac{-2}{5}+\left(\right.$ additive inverse of $\left.\frac{-5}{7}\right)$

$$
\begin{aligned}
& =\left(\frac{-2}{5}+\frac{5}{7}\right) \quad\left[\text { Q additive inverse of } \frac{-5}{7} \text { is } \frac{5}{7}\right] \\
& =\frac{(-14+25)}{35}=\frac{11}{35}
\end{aligned}
$$

Ex. The sum of two rational numbers is $\mathbf{- 5}$. If one of them is $\frac{-13}{6}$. Find the other
Sol. Let the other number be $x$. Then,


## PROPERTIES OF SUBTRACTION OF RATIONAL NUMBERS

(a) (Closure property) : If $\frac{\mathrm{a}}{\mathrm{b}}$ and $\frac{\mathrm{c}}{\mathrm{d}}$ are any two rational numbers, then $\frac{\mathrm{a}}{\mathrm{b}}-\frac{\mathrm{c}}{\mathrm{d}}$ is a rational number.

Ex. Consider the rational number $\frac{2}{3}$ and $\frac{1}{5}$
Sol. $\frac{2}{3}-\frac{1}{5}=\frac{10-3}{15}=\frac{7}{15}$
(b) (Commutative law) : The subtraction of rational numbers is not always commutative. That is for any two rational number $\frac{a}{b}$ and $\frac{c}{d}$. We have $\frac{a}{b}-\frac{c}{d}+\frac{c}{d}-\frac{a}{b}$

Ex. $\frac{2}{3}-\frac{1}{4}+\frac{1}{4}-\frac{2}{3}$

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Sol. $\frac{2}{3}-\frac{1}{4}=\frac{8-3}{12}=\frac{5}{12} \quad$ ค $\frac{1}{4}-\frac{2}{3}=\frac{3-8}{12}=\frac{-5}{12}$ P $\frac{2}{3}-\frac{1}{4}+\frac{1}{4}-\frac{2}{3}$
$p \frac{5}{12} \neq-\frac{5}{12}$ (Subtraction is not commutative for rational numbers.) LHS ${ }^{1}$ RHS
Ex. $\frac{2}{5}-\frac{3}{4}+\frac{3}{4}-\frac{2}{5}$ ค $\frac{2}{5}-\frac{3}{4}=\frac{8-15}{20}=\frac{-7}{20}$ ค $\frac{3}{4}-\frac{2}{5}=\frac{15-8}{20}=\frac{7}{20}$
$\frac{2}{5}-\frac{3}{4}+\frac{3}{4}-\frac{2}{5} \mathrm{p}-\frac{7}{20} \neq \frac{7}{20}$ (Subtraction is not commutative for rational numbers.)
(c) (Associative law) : The subtraction of rational number is not associative i.e. for any three rational numbers $\frac{a}{b}, \frac{c}{d}$ and $\frac{e}{f}$ we have $\left(\frac{a}{b}-\frac{c}{d}\right)-\frac{e}{f}+\frac{a}{b}-\left(\frac{c}{d}-\frac{e}{f}\right)$

Ex. $\left(\frac{2}{3}-\frac{4}{5}\right)-\frac{1}{2}=\left(\frac{10-12}{15}\right)-\frac{1}{2}$ P $\quad \frac{-2}{15}-\frac{1}{2}=\frac{-4-15}{30}=\frac{-19}{30}$
$\frac{2}{3}-\left(\frac{4}{5}-\frac{1}{2}\right)=\frac{2}{3}-\left(\frac{8-5}{10}\right) \quad$ ค $\quad \frac{2}{3}-\frac{3}{10}=\frac{20-9}{30}=\frac{11}{30}$

P $\left(\frac{2}{3}-\frac{4}{5}\right)-\frac{1}{2}, \frac{2}{3}-\left(\frac{4}{5}-\frac{1}{2}\right)$ (Subtraction is not associative for rational numbers.)
(d) (Existence of right Identity) : The rational number 0 is the right identity. That is, for any rational number $\frac{\mathbf{a}}{b}$, we have $\frac{\mathbf{a}}{\mathbf{b}}-\mathbf{0}=\frac{\mathbf{a}}{b}$

Ex. $\frac{3}{5}-0=\frac{3}{5}$

## -) MULTIPLICATION OF RATIONAL NUMBER :

For any two rational numbers $\frac{\mathrm{a}}{\mathrm{b}}$ and $\frac{\mathrm{c}}{\mathrm{d}}$, we define: $\left(\frac{\mathbf{a}}{\mathbf{b}} \times \frac{\mathbf{c}}{\mathbf{d}}\right)=\left(\frac{\mathbf{a} \times \mathbf{c}}{\mathbf{b} \times \mathbf{d}}\right)$

Ex. $\begin{array}{ll}\text { (i) } \frac{2}{3} \times \frac{-5}{7} & \text { (ii) } \frac{-7}{8} \times \frac{3}{5}\end{array}$
Sol. We have :
(i) $\frac{2}{3} \times \frac{-5}{7}=\frac{2 \times(-5)}{3 \times 7}=\frac{-10}{21}$
(ii) $\frac{-7}{8} \times \frac{3}{5}=\frac{(-7) \times 3}{8 \times 5}=\frac{-21}{40}$

Ex.
(i) $\frac{-3}{7} \times \frac{14}{5}$
(ii) $\frac{13}{6} \times \frac{-18}{91}$

Sol. We have:

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(i) $\frac{-3}{7} \times \frac{14}{5}=\frac{(-3) \times 14}{7 \times 5}=\frac{-6}{5}$
(ii) $\frac{13}{6} \times \frac{-18}{91}=\frac{13 \times(-18)}{6 \times 91}=\frac{-3}{7}$

## PROPERTIES OF MULTIPLICATION OF RATIONAL NUMBERS

(a) (Closure Property) : The product of two rational numbers is always a rational number.

If $\frac{\mathrm{a}}{\mathrm{b}}$ and $\frac{\mathrm{c}}{\mathrm{d}}$ are any two rational numbers than $\left(\frac{\mathbf{a}}{\mathbf{b}} \times \frac{\mathbf{c}}{\mathbf{d}}\right)$ is also a rational number.
Ex. (i) Consider the rational numbers $\frac{1}{2}$ and $\frac{5}{7}$. Then,

$$
\left(\frac{1}{2} \times \frac{5}{7}\right)=\frac{(1 \times 5)}{(2 \times 7)}=\frac{5}{14}, \text { which is a rational number. }
$$

(ii) Consider the rational numbers $\frac{-3}{7}$ and $\frac{5}{14}$. Then,

$$
\left(\frac{-3}{7} \times \frac{5}{14}\right)=\frac{(-3) \times 5}{7 \times 14}=\frac{-15}{98}, \text { which is a rational number. }
$$

(b) (Commutative law) : Two rational numbers can be multiplied in any order. Thus, for any rational number $\frac{\mathrm{a}}{\mathrm{b}}$ and $\frac{\mathrm{c}}{\mathrm{d}}$. We have $\left(\frac{\mathbf{a}}{\mathbf{b}} \times \frac{\mathbf{c}}{\mathbf{d}}\right)=\left(\frac{\mathbf{c}}{\mathbf{d}} \times \frac{\mathbf{a}}{\mathbf{b}}\right)$

Ex. (i) Let us consider the rational numbers $\frac{3}{4}$ and $\frac{5}{7}$. Then,

$$
\begin{aligned}
\left(\frac{3}{4} \times \frac{5}{7}\right) & =\frac{(3 \times 5)}{(4 \times 7)}=\frac{15}{28} \text { and }\left(\frac{5}{7} \times \frac{3}{4}\right)=\frac{(5 \times 3)}{(7 \times 4)}=\frac{15}{28} \\
1 \quad\left(\frac{3}{4} \times \frac{5}{7}\right) & =\left(\frac{5}{7} \times \frac{3}{4}\right) \bigcirc \text { LHS }=\text { RHS }
\end{aligned}
$$

(ii) Let us consider the rational numbers $\frac{-2}{5}$ and $\frac{6}{7}$. Then,

$$
\begin{aligned}
& \left(\frac{-2}{5} \times \frac{6}{7}\right)=\frac{(-2) \times(6)}{5 \times 7}=\frac{-12}{35} \text { and }\left(\frac{6}{7} \times \frac{-2}{5}\right)=\frac{6 \times(-2)}{7 \times 5}=\frac{-12}{35} \\
& \left(\frac{-2}{5} \times \frac{6}{7}\right)=\left(\frac{6}{7} \times \frac{-2}{5}\right) \quad \text { P LHS }=\text { RHS }
\end{aligned}
$$

(c) (Associative law) : While multiplying three or more rational numbers, they can be grouped in any order.

Thus, for any rational numbers $\frac{\mathrm{a}}{\mathrm{b}}, \frac{\mathrm{c}}{\mathrm{d}}$ and $\frac{\mathrm{e}}{\mathrm{f}}$, we have $\left(\frac{\mathbf{a}}{\mathbf{b}} \times \frac{\mathbf{c}}{\mathbf{d}}\right) \times \frac{\mathbf{e}}{\mathbf{f}}=\frac{\mathbf{a}}{\mathbf{b}} \times\left(\frac{\mathbf{c}}{\mathbf{d}} \times \frac{\mathbf{e}}{\mathbf{f}}\right)$
Ex. Consider the rational numbers $\frac{-5}{2}, \frac{-7}{4}$ and $\frac{1}{3}$. We have

Sol. $\left(\frac{-5}{2} \times \frac{-7}{4}\right) \times \frac{1}{3}=\left\{\frac{(-5) \times(-7)}{2 \times 4} \times \frac{1}{3}\right\}=\left(\frac{35}{8} \times \frac{1}{3}\right)=\frac{(35 \times 1)}{(8 \times 3)}=\frac{35}{24}$
and $\frac{-5}{2} \times\left(\frac{-7}{4} \times \frac{1}{3}\right)=\frac{-5}{2} \times \frac{(-7) \times 1}{4 \times 3}=\left(\frac{-5}{2} \times \frac{-7}{12}\right)=\frac{(-5) \times(-7)}{(2 \times 12)}=\frac{35}{24}$.
ค $\frac{35}{24}=\frac{35}{24} \quad$ P LHS $=$ RHS
(f) (Distributive law of multiplication over addition):

For any three rational numbers $\frac{\mathrm{a}}{\mathrm{b}}, \frac{\mathrm{c}}{\mathrm{d}}$ and $\frac{\mathrm{e}}{\mathrm{f}}$,
we have $\frac{\mathbf{a}}{\mathbf{b}} \times\left(\frac{\mathbf{c}}{\mathbf{d}}+\frac{\mathbf{e}}{\mathbf{f}}\right)=\left(\frac{\mathbf{a}}{\mathbf{b}} \times \frac{\mathbf{c}}{\mathbf{d}}\right)+\left(\frac{\mathbf{a}}{\mathbf{b}} \times \frac{\mathbf{e}}{\mathbf{f}}\right)$

Ex. Consider the rational numbers $\frac{-3}{4}, \frac{2}{3}$ and $\frac{-5}{6}$. We have
Sol. $\left(\frac{-3}{4}\right) \times\left\{\frac{2}{3}+\frac{-5}{6}\right\}=\left(\frac{-3}{4}\right) \times\left\{\frac{4+(-5)}{6}\right\}=\left(\frac{-3}{4}\right) \times\left(\frac{-1}{6}\right)=\frac{(-3) \times(-1)}{4 \times 6}=\frac{3}{24}=\frac{1}{8}$
Again, $\left(\frac{-3}{4}\right) \times \frac{2}{3}=\frac{(-3) \times 2}{4 \times 3}=\frac{-6}{12}=\frac{-1}{2}$ and $\left(\frac{-3}{4}\right) \times\left(\frac{-5}{6}\right)=\frac{(-3) \times(-5)}{4 \times 6}=\frac{15}{24}=\frac{5}{8}$
\ $\left(\frac{-1}{2}+\frac{5}{8}\right)=\frac{(-4+5)}{8}=\frac{1}{8}$
Hence, $\left(\frac{-3}{4}\right) \times\left\{\frac{2}{3}+\frac{-5}{6}\right\}=\left\{\left(\frac{-3}{4}\right) \times \frac{2}{3}\right\}+\left\{\left(\frac{-3}{4}\right) \times\left(\frac{-5}{6}\right)\right\}$
(g) (Multiplicative property of 0 ): For any rational number $\frac{\mathrm{a}}{\mathrm{b}}$,


## DO YOUR SELF

Verify the following statements : (a) $\left(\frac{7}{9}-\frac{11}{12}\right)+\frac{2}{3}=\frac{7}{9}-\left(\frac{11}{12}+\frac{2}{3}\right)$ (b) $\frac{3}{4}\left(\frac{2}{3}-\frac{1}{4}\right)=\frac{3}{4} \times \frac{2}{3}-\frac{3}{4} \times \frac{1}{4}$
(c) $\left(\frac{2}{3} \div \frac{3}{-5}\right) \div \frac{1}{2}=\frac{2}{3} \div\left(\frac{3}{-5} \div \frac{1}{2}\right)$
(d) Find $\frac{2}{5} \times \frac{-3}{7}-\frac{1}{14}-\frac{3}{7} \times \frac{3}{5}$

If $\frac{\mathrm{a}}{\mathrm{b}}$ and $\frac{\mathrm{c}}{\mathrm{d}}$ are two rational numbers such that $\frac{\mathrm{c}}{\mathrm{d}}{ }^{1} 0$,
we define $\left(\frac{\mathbf{a}}{\mathbf{b}} \div \frac{\mathbf{c}}{\mathbf{d}}\right)=\left(\frac{\mathbf{a}}{\mathbf{b}} \times \frac{\mathbf{d}}{\mathbf{c}}\right)$ when $\frac{\mathbf{a}}{\mathbf{b}}$ is divided by $\frac{\mathbf{c}}{\mathbf{d}}$, then $\frac{\mathbf{a}}{\mathbf{b}}$ is called the dividend; $\frac{\mathbf{c}}{\mathbf{d}}$ is called the divisor and the result is known as quotient.
Ex. Divide,
(i) $\frac{9}{16}$ by $\frac{5}{8}$
(ii) $\frac{-6}{25}$ by $\frac{3}{5}$
(iii) $\frac{11}{24}$ by $\frac{-5}{8}$
(iv) $\frac{-9}{40}$ by $\frac{-3}{8}$

Sol.
(i) $\frac{9}{16} \div \frac{5}{8}=\frac{9}{16} \times \frac{8}{5}=\frac{9 \times 8}{16 \times 5}=\frac{72}{80}=\frac{9}{10}$
(ii) $\frac{-6}{25} \div \frac{3}{5}=\frac{-6}{25} \times \frac{5}{3}=\frac{(-6) \times 5}{25 \times 3}=\frac{-30}{75}=\frac{-2}{5}$
(iii) $\frac{11}{24} \div \frac{-5}{8}=\frac{11}{24} \times \frac{8}{-5}=\frac{11 \times 8}{24 \times(-5)}=\frac{88}{-120}=\frac{-11}{15}$
(iv) $\frac{-9}{40} \div \frac{-3}{8}=\frac{-9}{40} \times \frac{8}{-3}=\frac{(-9) \times 8}{40 \times(-3)}=\frac{-72}{-120}=\frac{3}{5}$

Ex. The product of two numbers is $\frac{-28}{27}$. If one of the numbers is $\frac{-4}{9}$. Find the other.
Sol. Let the other number be x . Then,

$$
x \times \frac{-4}{9}=\frac{-28}{27}
$$

P $\quad x=\frac{-28}{27} \div \frac{-4}{9}=\frac{-28}{27} \times \frac{9}{-4}$
p $\quad \frac{(-28) \times 9}{27 \times(-4)}=\frac{-(28 \times 9)}{-(27 \times 4)}$
P $x=\frac{28 \times 9}{27 \times 4}=\frac{7}{3}$.
Hence, the other number is $\frac{7}{3}$.
Ex. 3 Fill in the blanks : $\frac{27}{16} \div(\ldots .)=.\frac{-15}{8}$

Sol.
Let $\frac{27}{16} \div\left(\frac{a}{b}\right)=\frac{-15}{8}$. Then,
$\frac{27}{16} \times \frac{b}{a}=\frac{-15}{8} \rho \frac{b}{a}=\frac{-15}{8} \times \frac{16}{27}=\frac{-10}{9} \rho \frac{a}{b}=\frac{9}{-10}$
Hence, the missing number is $\frac{-9}{10}$

## PROPERTIES OF DIVISION OF RATIONAL NUMBERS

Closure property : If $\frac{\mathrm{a}}{\mathrm{b}}$ and $\frac{\mathrm{c}}{\mathrm{d}}$ are any two rational numbers such that $\frac{\mathrm{c}}{\mathrm{d}}{ }^{1} 0$ then $\frac{\mathbf{a}}{\mathrm{b}} \div \frac{\mathbf{c}}{\mathrm{d}}$ is also a rational numbers.

Ex. $\frac{-6}{9} \div \frac{15}{-18}$

| Sot. We have$\frac{-6}{9} \div \frac{15}{-18}$ <br> $\frac{-6}{9} \times \frac{-18}{15}=\frac{4}{5} . \quad$ (The quotient <br> But also a rational number.) <br> But $\quad \frac{6}{9} \div 0=?$ |
| :--- |
| The answer is not defined, so rational numbers are not closed under division. |

(A) For any rational number $\frac{\mathrm{a}}{\mathrm{b}}$, we have
(B) For every non-zero rational number $\frac{\mathrm{a}}{\mathrm{b}}$, We have
$\frac{\mathrm{a}}{\mathrm{b}} \div 1=\frac{\mathrm{a}}{\mathrm{b}}$ and $\frac{\mathrm{a}}{\mathrm{b}} \div(-1)=\frac{-\mathrm{a}}{\mathrm{b}}$
(i) $\frac{\mathrm{a}}{\mathrm{b}} \div \frac{\mathrm{a}}{\mathrm{b}}=\frac{\mathrm{a}}{\mathrm{b}} \times \frac{\mathrm{b}}{\mathrm{a}}=1$
(ii) $\frac{\mathrm{a}}{\mathrm{b}} \div\left(\frac{-\mathrm{a}}{\mathrm{b}}\right)=\frac{\mathrm{a}}{\mathrm{b}} \times \frac{\mathrm{b}}{-\mathrm{a}}=-1$

Remark : The division of rational number is neither commutative nor associative.

## REPRESENTATION OF RATIONAL NUMBERS ON THE NUMBER LINE

We have learnt how to represent integers on the number line.
Draw any line. Take a point $O$ on it. Call it 0 (zero). Set of equal distances on the right as well as on the left of O. Such a distance is known as a unit length. Clearly, the points $A, B, C, D$ represent the integers $1,2,3,4$ respectively and the point $A^{\prime}, B^{\prime}, C^{\prime} D^{\prime}$ represent the integers $-1,-2,-3,-4$ respectively

| E | D | C | B' | A' | O | A | B | C | D | E |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| -5 | 4 | -3 | -2 | -1 | 0 |  | 2 | 3 | 4 | 5 |  |

Thus, we may represent any integer by a point on the number line. Clearly, every positive integer lies to the right of $O$ and every negative integer lies to the left of $O$.
Similarly we can represent rational numbers.
Ex. Represent $\frac{1}{2}$ and $-\frac{1}{2}$ on the number line.
Sol. Draw a line. Take a point $O$ on it. Let it represent 0 . Set off unit length $O A$ and $O A$ ' to the right as well as to the left of $O$.
The, A represents the integer 1 and $\mathrm{A}^{\prime}$ represents the integer -1 .


Now, divide OA into two equal parts. Let OP be the first part out of these two parts.
Then, the point P represents the rational number $\frac{1}{2}$.
Again, divide OA' into two equal parts. Let OP' be the first part out of these 2 parts. Then the point $P^{\prime}$ represents the rational number $-\frac{1}{2}$
Ex. Represent $\frac{4}{7}$ on number line.
Sol. Divide the line segment between 0 and 1 into 7 equal parts (because $\frac{4}{7}$ lies between 0 and 1 )


Ex. Represent $\frac{-9}{5}$ on number line.

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Divide the line segment between -1 and -2 (because $-1 \frac{4}{5}$ lies between -1 and -2 ) into 5 equal parts


COMPETITION WINDOW

(ii) Non terminating \& repeating decimals : Visualize $4 . \overline{26}$ on the number line, up to 4 decimals places. $4 . \overline{26}=4.262626 \ldots$


DO YOUR SELF
Represent each of the following numbers on the number line :
(i) $\frac{-1}{3}$
(ii) $\frac{-3}{4}$
(iii) $-1 \frac{2}{3}$
(iv) $\frac{17}{6}$
(v) -3
(vi) $\frac{23}{5}$

FINDING RATIONAL NUMBER BETWEEN TWO NUMBERS
(A) $1^{\text {st }}$ method : Find a rational number between $x$ and $y$ then, $\frac{x+y}{2}$ is a rational number lying between $x$ and $y$.
(B) $\quad 2^{\text {nd }}$ method : Find $n$ rational number between $x$ and $y$ (when $x$ and $y$ is non fraction number) then we use formula.

$$
\frac{x(n+1)}{n+1}, \frac{y(n+1)}{n+1}
$$

(C) $3^{\text {rd }}$ method : Find n rational number between x and y (when x and y is fraction Number) then we use formula

$$
d=\frac{(y-x)}{n+1}
$$

then $n$ rational number lying between $x$ and $y$ are $(x+d),(x+2 d),(x+3 d) \ldots . .(x+n d)$

Remark : $\quad x=$ First Rational Number, $y=$ Second Rational Number, $n=$ No. of Rational Number
Ex. Find one rational number between $\frac{1}{3}$ and $\frac{1}{2}$
Sol. $x=\frac{1}{3} ; y=\frac{1}{2} p \frac{x+y}{2}=\frac{\frac{1}{3}+\frac{1}{2}}{2}=\frac{2+3}{6 \times 2}=\frac{5}{12}$

## Ex Find 4 rational numbers between 4 and 5 .

Sol. $x=4, y=5, n=4$
$\frac{\mathbf{x} \times(\mathbf{n}+1)}{\mathbf{n}+1}=\frac{4 \times(4+1)}{4+1}=\frac{4 \times 5}{5}=\frac{20}{5}$
$\frac{\mathbf{y} \times(\mathbf{n}+\mathbf{1})}{\mathbf{n}+1}=\frac{5 \times(4+1)}{4+1}=\frac{5 \times 5}{5}=\frac{25}{5}$
$\frac{20}{5},\left[\frac{21}{5}, \frac{22}{5}, \frac{23}{5}, \frac{24}{5}\right], \frac{25}{5}$
Ex Find 3 rational number between $\frac{6}{5}, \frac{7}{5}$
Sol. $x=\frac{6}{5}, y=\frac{7}{5}, n=3$
$\mathbf{d}=\left(\frac{y-x}{n+1}\right)=\frac{\frac{7}{5}-\frac{6}{5}}{3+1}=\left(\frac{\frac{7-6}{5}}{4}\right)=\left(\frac{1}{20}\right)$
$\mathbf{x}+\mathbf{d}=\frac{6}{5}+\frac{1}{20}=\frac{24+1}{20}=\frac{25}{20}$
$x+2 d=\frac{6}{5}+2 \times \frac{1}{20}=\frac{24+2}{20}=\frac{26}{20}$
$x+3 d=\frac{6}{5}+\frac{3}{20}=\frac{24+3}{20}=\frac{27}{20}$
$\frac{24}{20},\left[\frac{25}{20}, \frac{26}{20}, \frac{27}{20}\right], \frac{28}{20}$

## DO YOUR SELF

(i) Find a rational number between -2 and 6 .
(ii) Find 29 rational numbers between $\frac{-2}{5}$ and $\frac{1}{5}$
(iii) Insert 5 rational numbers between $-\frac{1}{3}$ and $\frac{1}{2}$
(iv) Find two rational numbers between -3 and -2 .

## అ ఔ ఒ もఇ వి ఖీ వి ఖీ ఔ ఓ థ్వ ఓ ఆ ఔ థ゙





$$
\left\lvert\, \Phi=\left\{\begin{array}{c}
x \text { if } x \geq 0 \\
-x \text { if } x<0
\end{array}\right.\right.
$$

ఇ．ס．$|\square 7|=7,|3|=3$ ，జొఖి．
$0 ట, \odot, \quad ఒ ひ ి \Phi\{\{\square \square \Phi\}=\mid \Phi$
ఒఝై$\square \square=\mid \Phi$
ఒยఆజ $\sqrt{(\mathrm{x})^{2}}=\mid \Phi$

## 

（土） $\mid$ ひิ｜$=\mid \square$ ひิ｜
（山） $\mid$ జิழ｜＝｜ชิ｜｜ $\mid$
（ఋ）$\quad\left|\frac{\mathrm{a}}{\mathrm{b}}\right|=\frac{|\mathrm{a}|}{|\mathrm{b}|}$





## DO YOUR SELF

గిజీజిథి ణు，జిణ｜థ＋థ｜$\leq|\Phi+|థ|$ జిఱి $\square$
$\begin{array}{ll}\text {（3）} \Phi=\frac{-9}{7}, \Phi=\frac{3}{4} & \text {（د）} \Phi=\frac{8}{-3}, \Phi=\frac{-7}{9}\end{array}$
तిజ్మిజిథ ణు，జిణ $\mid \Phi{ }_{\circ}$ 甲｜$=\left|\Phi{ }_{\odot}\right| థ \mid$ జిత్య
（0）$甲=\frac{3}{4}, 甲=\frac{-1}{2}$
（د）$\Phi=\frac{-7}{8}, \Phi=\frac{1}{-4}$

## 







ఇ甲 $\frac{3}{4}=0.75, \frac{8}{10}=0.8, \frac{1}{4}=0.25$



ఇq $\frac{8}{3}=2.666 \ldots=2 . \overline{6}$

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 జజ్ిటటబి టీ，


## ఆఖఖఇఅఖి ఒఇఖిలుฎఙఆ

$\left(\frac{\mathbf{p}}{\mathbf{q}}\right)$ form $=\frac{\text {（Complete numbers）}-(\text { numberformed by Non－repeating digit）}}{\text { No．of9 as no．of repeating digits after that write no．of } 0 \text { as no．of non repeating digits．}}$
ఇゅ．（ง）
$0 . \overline{35}=\frac{35-0}{99}=\frac{35}{99}$
（ふ） $0.4 \overline{35}=\frac{435-4}{990}=\frac{431}{990}$
（凶） $23 . \overline{43}=\frac{2343-23}{99}=\frac{2320}{99}$

య๘ట．ఎజఱ థ＝ $23 . \overline{43}$ ขి，జీి，
$\Rightarrow \Phi=23.434343 \ldots$



$$
100 \Phi=2343.4343 \ldots
$$

（凶）


$$
100 \Phi \square \Phi=(2343.4343 \ldots) \square(23.4343 \ldots)
$$

$\Rightarrow 99 \Phi=2320$
$\Rightarrow 甲=\frac{2320}{99}$

戸జ $৩, ఙ{ }^{〔} \approx$

$$
23 . \overline{43}=23+0 . \overline{43}
$$


$\Rightarrow \quad 23 . \overline{43}=\frac{23 \times 99+43}{99}$

$$
=\frac{2277+43}{99}=\frac{2320}{99}
$$

 జ Јヨ্̧ Јఠట ．

2ఠట．จిు，$p, ~ ి ి జ ~ ు, జ ి ~ ఔ ు ~$
$\frac{2}{7}=2$ 。 $\frac{1}{7}=0 . \overline{285714}$
$\frac{3}{7}=3 \cdot \frac{1}{7}=0 . \overline{428571}$
$\frac{4}{7}=4 \odot \frac{1}{7}=0 . \overline{571428} \quad ; \quad \frac{5}{7}=5 \odot \frac{1}{7}=0 . \overline{714285}$

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 ఒిటిజ ๘ $=0$.
æ 2





## 



 ట్రటెణఠటిజ్




 $\left[\mathrm{Q}(\sqrt[3]{\mathrm{a}})^{3}+(\sqrt[3]{\mathrm{b}})^{3}\right]=\mathrm{a}+\mathrm{b}$ ఆฺభి, , థిఙిణฮటిబిట.


(ง) $\sqrt{10}$
(3) $\sqrt{162}$
((1)) $\sqrt[3]{4}$
(ङ) $\sqrt[3]{16}$

20ట. (ง) $\sqrt{10}$

(w) $\sqrt{162}$

ขజిణజటిజిటషబిం జిజిఢిణఁత జ $\sqrt{2}, \sqrt{2}$

(()) $\sqrt[3]{4}$
$\Rightarrow \sqrt[3]{4}$ 。 $\sqrt[3]{4^{2}}=\sqrt[3]{4^{3}}=4$

(3) $\sqrt[3]{16}$

ขభలిటజ్థొ జితిట ๔ి $\sqrt[3]{16}, 2 \sqrt[3]{2}$



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ఇ甲（土）$\frac{189}{125}=\frac{189}{5^{3}}=\frac{189}{2^{0} \times 5^{3}}$.

（山）$\frac{17}{6}=2.83333 \ldots \ldots$



（山）$\frac{17}{8}=\frac{17}{2^{3} \times 5^{0}}$


（3）$\frac{64}{455}=\frac{64}{5 \times 7 \times 13}$
 โి జిజిఁిణฝీం）

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## SOLVED EXAMPLES


（i）$\frac{x}{4}, \frac{16}{12}$
（a）$\frac{-4}{5}, \frac{x}{10}$
2003.

$$
\text { (د) } \begin{aligned}
& \frac{x}{4}=\frac{16}{12} \\
& \Rightarrow 甲 \odot 12=4 \circ 16 \\
& \Rightarrow \Phi=\frac{4 \times 16}{12}=\frac{16}{3}
\end{aligned}
$$

（ سలmటి ）
（ఢ甲 ழిడిథ ఠిడిజజఙభిణ ఐిశో
（๗）$\frac{-4}{5}=\frac{x}{10}$

$$
\Rightarrow 5_{\odot} \Phi=(\square 4){ }_{\odot} 10 \quad \Rightarrow \Phi=\frac{-4 \times 10}{5}=\square 8
$$

ఇ甲． 2 อజజ $\frac{7}{9}$ ๕ిటిజ $\frac{-12}{9}$
20ట．戸జ ৩，ఒి ङ，

$$
\frac{7}{9}+\frac{-12}{9}=\frac{7+(-12)}{9}=\frac{-5}{9} \quad[\rightarrow 7+(\square 12)=\square 5]
$$





ఐఅఒ ๔్జి 4 జిటిజ $6=12$ ．
$\therefore \frac{3}{-4}=\frac{(-3) \times 3}{4 \times 3}=\frac{-9}{12}$ ఒิటిజ $\frac{-5}{6}=\frac{(-5) \times 2}{6 \times 2}=\frac{-10}{12}$
అటజజిడిటథ，$\frac{-9}{12}>\frac{-10}{12}$ ．ల๐జటిథిజ，$\frac{3}{-4}>\frac{-5}{6}$
ఇ甲． 4 ฉผอటైిథ ：$\frac{-8}{-15}+\frac{4}{-3}$
20ట．

$$
\frac{8}{-15}+\frac{4}{-3}=\frac{-8}{15}+\frac{-4}{3}
$$

$$
\left[Q \frac{8}{-15}=\frac{8 \times-1}{(-15) \times(-1)}=\frac{-8}{15} \text { and } \frac{4}{-3}=\frac{4 \times-1}{(-3) \times(-1)}=\frac{-4}{3}\right]
$$

ఐఅఒ త్జి 15 జిటిజ 3 ， 15


$$
\begin{aligned}
& \frac{-4}{3}=\frac{-4 \times 5}{3 \times 5}=\frac{-20}{15} \\
\therefore \quad & \frac{-8}{15}+\frac{4}{-3}=\frac{-8}{15}+\frac{-4}{3} \\
& =\frac{-8}{15}+\frac{-20}{15} \\
& =\frac{(-8)+(-20)}{15}=\frac{-28}{15}
\end{aligned}
$$

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ఇ థ． 5 तิజสమిథ ：$\left(\frac{\mathrm{a}}{\mathrm{b}}+\frac{\mathrm{c}}{\mathrm{d}}\right)+\frac{\mathrm{e}}{\mathrm{f}}=\frac{\mathrm{a}}{\mathrm{b}}+\left(\frac{\mathrm{c}}{\mathrm{d}}+\frac{\mathrm{e}}{\mathrm{f}}\right)$ జิఱฺ $\frac{\mathrm{a}}{\mathrm{b}}=\frac{-2}{3}, \frac{\mathrm{c}}{\mathrm{d}}=\frac{5}{7}$ జిటะ $\frac{\mathrm{e}}{\mathrm{f}}=\frac{-1}{6}$


$$
\begin{aligned}
& \left(\frac{\mathrm{a}}{\mathrm{~b}}+\frac{\mathrm{c}}{\mathrm{~d}}\right)+\frac{\mathrm{e}}{\mathrm{f}}=\left(\frac{-2}{3}+\frac{5}{7}\right)+\frac{-1}{6} \Rightarrow \frac{(-2) \times 7+3 \times 5}{21}+\frac{-1}{6}=\frac{(-14)+15}{21}+\frac{-1}{6} \\
& \Rightarrow \frac{1}{21}+\frac{(-1)}{6}=\frac{1 \times 2+(-1) \times 7}{42}=\frac{2+(-7)}{42}=\frac{(-5)}{42}=\frac{-5}{42} \\
& \text { 2ӊటะ, } \frac{\mathrm{a}}{\mathrm{~b}}+\left(\frac{\mathrm{c}}{\mathrm{~d}}+\frac{\mathrm{e}}{\mathrm{f}}\right)=\frac{-2}{3}+\left(\frac{5}{7}+\frac{-1}{6}\right) \Rightarrow \frac{-2}{3}+\frac{5 \times 6+7 \times(-1)}{42}=\frac{-2}{3}+\frac{30+(-7)}{42} \\
& \Rightarrow \frac{(-2)}{3}+\frac{23}{42}=\frac{(-2) \times 14+23 \times 1}{42}=\frac{(-28)+(23)}{42}=\frac{(-5)}{42}=\frac{-5}{42} \\
& \therefore\left(\frac{\mathrm{a}}{\mathrm{~b}}+\frac{\mathrm{c}}{\mathrm{~d}}\right)+\frac{\mathrm{e}}{\mathrm{f}}=\frac{\mathrm{a}}{\mathrm{~b}}+\left(\frac{\mathrm{c}}{\mathrm{~d}}+\frac{\mathrm{e}}{\mathrm{f}}\right)
\end{aligned}
$$




$$
\therefore \quad \frac{-5}{7} \square\left(\frac{-3}{8}\right)=\frac{-5}{7}+\frac{3}{8}=\frac{(-5) \times 8+3 \times 7}{56}=\frac{-40+21}{56}=\square \frac{19}{56}
$$




$$
\begin{aligned}
& \frac{-5}{8}+\Phi=\frac{5}{9} \\
& \Rightarrow \Rightarrow \quad \Phi=\frac{5}{9} \square\left(\frac{-5}{8}\right) \quad\left[\text { Transposing } \frac{-5}{8} \text { to RHS }\right] \\
& \Rightarrow=\frac{5}{9}+\frac{5}{8} \quad \Rightarrow \quad \Phi=\frac{5 \times 8+5 \times 9}{72}=\frac{40+45}{72}=\frac{85}{72}
\end{aligned}
$$




$$
\begin{aligned}
& \frac{-3}{4} \square 甲=\frac{5}{6} \quad \Rightarrow \quad \frac{-3}{4} \square \frac{5}{6}=甲 \quad\left[\text { Transposing } x \text { to RHS and } \frac{5}{6} \text { to LHS }\right] \\
& \Rightarrow \Phi=\frac{-3}{4} \square \frac{5}{6} \quad \Rightarrow \Phi=\frac{-3}{4}+\frac{-5}{6} \quad\left[\mathrm{Q}-\frac{5}{6}=\frac{-5}{6}\right] \\
& \Rightarrow \Phi=\frac{(-3) \times 3+(-5) \times 2}{12} \\
& \Rightarrow \Phi=\frac{(-9)+(-10)}{12}=\frac{-19}{12} \quad[7 \quad \text { ఐఅఒ జి } 4 \text { జిటిజ } 6 \text { P 12] }
\end{aligned}
$$

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ఇ థ． 9 ఇ๙ษటสีใణజ：$\frac{6}{7} \square 2+\frac{-7}{9}+\frac{19}{21}$


| 7 | 7, | 1, | 9, | 21 |
| :--- | :--- | :--- | :--- | :--- |
| 3 | 1, | 1, | 9, | 3 |
|  | 1, | 1, | 3, | 1 |

$=\frac{6}{7}+\frac{(-2)}{1}+\frac{(-7)}{9}+\frac{19}{21}$
$\therefore$ ఐఅఒ $=7$ 。3。3 $=63$
$=\frac{6 \times 9+(-2) \times 63+(-7) \times 7+19 \times 3}{63}$
$=\frac{54+(-126)+(-49)+57}{63}=\frac{111+(-175)}{63}=\frac{-64}{63}$

ఇ థ． 10 2xటొలటజిథి ：
（3）$\frac{-2}{3}+\frac{5}{9} \square \frac{-7}{6}$
（3）$\frac{5}{12}+\frac{-5}{18} \square \frac{7}{24}$
20ట．（Ј）థజ ৩，ఒి ఔ

$$
\begin{aligned}
& \frac{-2}{3}+\frac{5}{9} \square \frac{-7}{6}=\frac{-2}{3}+\frac{5}{9} \square \frac{7}{6} \\
& =\frac{(-2) \times 6+5 \times 2+7 \times 3}{18} \\
& =\frac{-12+10+21}{18}=\frac{-12+31}{18}=\frac{19}{18}
\end{aligned}
$$

$$
\left[\mathrm{Q}-\left(\frac{-7}{6}\right)=\frac{7}{6}\right]
$$

$$
=\frac{(-2) \times 6+5 \times 2+7 \times 3}{18} \quad[\neg \text { ఐఅఒ ๕జ 3, 9, జిటిజ } 6,18]
$$

（山）థజజ ৩，ఒి ఔ

20ట．ม． $212 \frac{1}{3}=\frac{637}{3}$
ழిథ్ తి 1 ట థిటఱ్య．$=\frac{637}{3} \div \frac{49}{4}=\frac{637}{3} \odot \frac{4}{49}=\frac{52}{3}=$ 2．． $17 \frac{1}{3}$
ఇ． 12 బยอటజిథ $\left(\frac{-7}{18} \times \frac{15}{-7}\right) \square\left(1 \times \frac{1}{4}\right)+\left(\frac{1}{2} \times \frac{1}{4}\right)$
20ట．$\left(\frac{-7}{18} \times \frac{15}{-7}\right) \square\left(1 \times \frac{1}{4}\right)+\left(\frac{1}{2} \times \frac{1}{4}\right)=\left(\frac{-7}{18} \times \frac{15}{-7}\right) \square\left(\frac{1}{1} \times \frac{1}{4}\right)+\left(\frac{1}{2} \times \frac{1}{4}\right)$
$=\frac{-7 \times 15}{18 \times-7} \square \frac{1 \times 1}{1 \times 4}+\frac{1 \times 1}{2 \times 4}=\frac{1 \times 5}{6 \times 1} \square \frac{1 \times 1}{1 \times 4}+\frac{1 \times 1}{2 \times 4}$
$=\frac{5}{6} \square \frac{1}{4}+\frac{1}{8}=\frac{5}{6}+\frac{-1}{4}+\frac{1}{8}$

$$
\left[\mathrm{Q}-\frac{1}{4}=\frac{-1}{4}\right]
$$

$=\frac{5 \times 4+(-1) \times 6+1 \times 3}{24}=\frac{20+(-6)+3}{24}=\frac{17}{24}$

$$
\begin{aligned}
& \frac{5}{12}+\frac{-5}{18} \square \frac{7}{24}=\frac{5}{12}+\frac{-5}{18}+\frac{-7}{24} \\
& {\left[Q-\frac{7}{24}=\frac{-7}{24}\right]} \\
& =\frac{5 \times 6+(-5) \times 4+(-7) \times 3)}{72} \\
& =\frac{30+(-20)+(-21)}{72}=\frac{30+(-41)}{72}=\frac{-11}{72} \\
& \text { [ } \dagger \text { ఏ ఐఅఒ జిజి } 12,18 \text { జిటిజ } 24 \text { p 72] }
\end{aligned}
$$

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$$
\begin{aligned}
& \frac{-3}{5} \odot\left(-\frac{10}{9}\right) \odot\left(\frac{21}{-4}\right) \circ(\square 6)=\frac{-3}{5} \odot \frac{-10}{9} \odot \frac{21}{-4} \odot \frac{-6}{1} \\
& \Rightarrow \frac{(-3) \times(-10) \times 21 \times(-6)}{5 \times 9 \times(-4) \times 1}=\frac{-(3 \times 10 \times 21 \times 6)}{-(5 \times 9 \times 4 \times 1)}=\frac{3 \times 10 \times 21 \times 6}{5 \times 9 \times 4} \\
& \Rightarrow \frac{1 \times 5 \times 21 \times 6}{5 \times 3 \times 2}=\frac{1 \times 1 \times 7 \times 3}{1 \times 1 \times 1}=21
\end{aligned}
$$




2003.
()) $\frac{3}{5} \div \frac{4}{25}=\frac{3}{5} \circ \frac{25}{4}=\frac{3 \times 25}{5 \times 4}=\frac{3 \times 5}{1 \times 4}=\frac{15}{4}$
(๗) $\frac{-8}{9} \div \frac{4}{3}=\frac{-8}{9} \circ \frac{3}{4}=\frac{-8 \times 3}{9 \times 4}=\frac{-2 \times 1}{3 \times 1}=\frac{-2}{3}$



$=\Phi_{\odot} \frac{14}{27}=\square \frac{28}{81}$
$\Phi=\frac{-(28 \times 27)}{81 \times 14}=\frac{-(2 \times 1)}{3 \times 1}=\frac{-2}{3}$



$=\frac{3}{-14} \odot 甲=\frac{5}{12}$


## 



(0) $\square \frac{7}{48}$
(ஃ) $\frac{1}{24}$
(అ) $\frac{13}{48}$
(अ) $\frac{1}{3}$

(o) $\square \frac{19}{60}$
(ஃ) $\frac{-11}{30}$
(అ) $\frac{51}{60}$
(ఆ) $\frac{1}{20}$


(0) $\frac{-11}{28}$
(ஃ) $\frac{-5}{7}$
(అ) $\frac{9}{-14}$
(अ) $\frac{29}{-42}$

(0) $-\frac{7}{5}$
(ஃ) $\square \frac{13}{5}$
(అ) $\frac{13}{5}$
(ङ) $\frac{7}{5}$

(0) $\frac{-12}{26}$
(ஃ) $\frac{-49}{91}$
(అ) $\frac{-9}{16}$
(अ) $\frac{28}{-105}$

(0) $\frac{-13}{3}$
(\%) $\frac{-19}{3}$
(అ) $\frac{1}{3}$
(ఆ) $\frac{13}{3}$
7. 2ిజ జษటสజి జి $\left(-\frac{9}{16} \times \frac{8}{15}\right)$, :
(o) $\square \frac{3}{10}$
(ஃ) $\square \frac{4}{15}$
(అ) $\square \frac{9}{25}$
(↔) $\square]$





9. 2ัజ 飞๖టสు $\left(\frac{-5}{9} \div \frac{2}{3}\right)$, :-
(0) $\square \frac{5}{2}$
(ஃ) $\square \frac{5}{6}$
(అ) $\square \frac{10}{27}$
(ङ) $\square \frac{6}{5}$
10. ఈ\&
(o) $\square \frac{32}{45}$
(ஃ) $\square \frac{8}{5}$
(అ) $\square \frac{9}{10}$
(ఆ) $\square \frac{5}{6}$


1．గటిర ఒిఠఠడిఠిఠిజిణజ ఠిిఠిజిణఝ జిటిజ．
（））$\square \frac{2}{3} \times \frac{3}{5}+\frac{5}{2}-\frac{3}{5} \times \frac{1}{6}$
（3）$\frac{2}{5} \times\left(-\frac{3}{7}\right)-\frac{1}{6} \times \frac{3}{2}+\frac{1}{14} \times \frac{2}{5}$

（3）$\frac{2}{8}$
（3）$\frac{-5}{9}$
（अ）$\frac{-6}{-5}$
（ख）$\frac{2}{-9}$
（ㄹ）$\frac{19}{-6}$

3． กิజ్జిజిథి ణుజిణ $\square(\square థ)=థ$ జిత్మి．
（3）$甲=\frac{11}{15}$
（『）$\Phi=\square \frac{13}{17}$

（3） $\square \quad 13$
（অ）$\frac{-13}{19}$
（（））$\frac{1}{5}$
（ङ）$\frac{-5}{8} \times \frac{-3}{7}$
（ㄹ）$\square$
$1 \cdot \frac{-2}{5}$
（ब）$\square 1$

（3）$\frac{-4}{5}=1=1 \circ \frac{-4}{5}=$
$\square \frac{4}{5}$
（د）$\square \frac{13}{17} \times \frac{-2}{7}=\frac{-2}{7} \times \frac{-13}{17}$
（®）$\frac{-19}{29} \times \frac{29}{-19}=1$
6．2๔ణణిబిழిణ ：（3）$\frac{2}{5}$ from $\frac{1}{15}$
（د）$\frac{-3}{7}$ from $\frac{12}{14}$
（®）$\frac{-7}{12}$ from $\frac{-5}{18}$

7．खயీటీజిథ ：（د）$\frac{7}{42}-\frac{8}{21}$
（د）$\frac{2}{15}-\frac{-4}{5}$
（『）$\frac{-7}{12}-\frac{-8}{15}$
（コ）$\frac{5}{24}-\frac{-17}{-36}$
（ㄹ）$\frac{-8}{15}-\frac{5}{18}$
（ङ）$\frac{2}{9}-\frac{-5}{12}$




（๖）అజిటి తిజ జઉఔజ 1 ழฺ 0？

（د）$\square \frac{2}{15}-\left(\frac{-7}{12}\right)=\ldots+\frac{7}{12}$

12．2ӊలిటిథ ：（ง）$\left(\frac{2}{3} \times \frac{15}{-16}\right) \square\left(\frac{7}{12} \times \frac{-24}{35}\right) \quad$（د）$\left(\frac{5}{7} \times \frac{-14}{15}\right)+\left(\frac{-8}{15} \times \frac{3}{-16}\right) \square\left(\frac{2}{9} \times \frac{-27}{16}\right)$

13．గిజీజిథి ణుజ జితటటృతిటిం：
（）$\frac{2}{3} \times \frac{5}{6}=\frac{5}{6} \times \frac{2}{3}$
（د）$\frac{-34}{48} \times \frac{16}{17}=\frac{16}{17} \times \frac{-34}{48}$
（®）$\frac{-9}{20} \times \frac{35}{-27}=\frac{35}{-27} \times \frac{-9}{20}$



## 

## 

1. గిజ్మిథి ణుజ జిథటటతికిం: (i) $\frac{2}{3} \times\left(\frac{3}{5} \times \frac{25}{18}\right)=\left(\frac{2}{3} \times \frac{3}{5}\right) \times \frac{25}{18} \quad$ (()) $\frac{14}{15} \times\left(\frac{-3}{12} \times \frac{22}{-33}\right)=\left(\frac{14}{15} \times \frac{-3}{12}\right) \times \frac{22}{-33}$



(3) $\frac{-35}{17} \div 1=\ldots$
(®) $\frac{2}{3} \div \ldots=-\frac{2}{3}$
(®) $\frac{25}{18} \div \frac{-25}{18}=\ldots$
(®) $\frac{18}{17} \div \ldots=1$
()ㅏ $\left(\frac{3}{5}-\frac{1}{2}\right)+\ldots=\frac{3}{5} \div \frac{3}{4}-\frac{1}{2} \div \frac{3}{4} \quad$ (ㅎ) $\frac{5}{6} \div \frac{2}{-3}=\frac{5}{6} \times \ldots$


(a) $\frac{13}{5} \div \frac{26}{10}=\frac{26}{10} \div \frac{13}{5} \quad$ (®) $\left(\frac{5}{9} \div \frac{1}{3}\right) \div \frac{5}{2}=\frac{5}{9} \div\left(\frac{1}{3} \div \frac{5}{2}\right)$


(2) $\left(\frac{8}{15}+\frac{6}{5}\right)-\frac{5}{12}=\frac{8}{15}+\left(\frac{6}{5}-\frac{5}{12}\right)$
(د) $8 \square\left(2 \frac{3}{5}+2 \frac{5}{12}\right)=8$
$\square 2 \frac{3}{5}-2 \frac{5}{12}$
(』) $\frac{5}{2} \square 0$
$0=0$
$\square \frac{5}{2}$



## 

11. నயీటమిథ : $\frac{4}{3}+\frac{3}{5}+\frac{-2}{3}+-\frac{11}{5}$






18 .




23 ．
 8000，0，0，
 జుు ，ుజ，ఠజజీజ？
26．ะథి ణజిఇగకం థ＝$\frac{-3}{4}, ~ థ ి=\frac{2}{3}$ జీటిజ $ద=\frac{-5}{6}$ ，జజమిథి ణ，జిణ ：
（0）$\Phi_{\odot}(\Phi+\omega)=\Phi_{\circ} 甲+\Phi_{\circ} \omega$


（ङ）$\uparrow$ 。 $\omega=\omega_{\circ}$ 甲

















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|  |  |  |
| :---: | :---: | :---: |

ఇずఇขఅఖขฐー 1

1．అ
2． 0
3． 0
4．↔
5．๑
6．๒
7． 0
8．：
9．：
10．ஆ



7．（অ）$-\frac{3}{14}$ ，（অ）$\frac{14}{15}$, （অ）$-\frac{1}{20}$ ，（ङ）$-\frac{19}{72}$, （ङ）$-\frac{73}{90}$ ，（ङ）$\frac{23}{36}$
8．（3）$\frac{11}{12}$ ，（د）$\frac{23}{36}$ ，（『）$-\frac{7}{48}$ ，

11．（3）$-\frac{9}{8}$, （अ）$\frac{4}{11}$, （अ）$\frac{3}{4}$, （उ）$-\frac{5}{2}$ ，
12．（3）$-\frac{5}{2}$, （3）$-\frac{9}{40}$ ，

14．（3）$>$ ，（অ）$=$ ，（『）
15．（ง）$-\frac{2}{7}$, （3）$\frac{4}{7}$, （『）$-\frac{3}{8}$
ఇఖఇఖఅఖఖఇー2

3．（3）$-\frac{3}{4}$, （3）$\square 2$ ，（ञ）$\frac{9}{2}$
5．（3）$-\frac{16}{15}$, （3）$-\frac{128}{7}$, （अ）$-\frac{2}{21}$, （ङ）$-\frac{32}{75}$
6．（ఎ）ఈజిటిజ（ゝ）なజిటిజ



22．$\frac{7}{8}$ Litre
23． 60 ๗ట
24． $42 \frac{1}{4}$
25．ఖ． $149 \frac{5}{8}$
27．$\square 15 \quad$ 28．$-\frac{56}{15}$
29． 14 ，પిలి
30．$\frac{7}{4} \quad 31 . \quad 2 . \frac{19}{2}$
32．$\frac{25}{3} \mathrm{~m}$
33．2．$\frac{45}{2}$
34． $159 \frac{1}{2}$
40．$\frac{3}{4}$
41．$\frac{4}{3}$
42．$\frac{8}{3}$
43．$\square \frac{3}{16}$
44．$\frac{3}{4}$
45．$\frac{2}{5}$
46．$\frac{97}{33}$
47．$-1 \frac{11}{15}$
48．$-\frac{7}{5}$
49．$\frac{59}{30}$
50．$\frac{1}{4}$

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## 






















18 .


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## 





(ఆ) ఓతటిజ తజి ణు,జ్జు
2.

(o) $\frac{2}{3}$
(ஃ) $\frac{3}{5}$
(అ) $\frac{4}{5}$
(अ) $\frac{1}{2}$

(o) 6,3
(\%) 7, 3
(అ) 8,3
(ఆ) 11,3

(o) $\frac{-2}{3}<\frac{4}{-9}<\frac{-5}{12}<\frac{7}{-18}$
(ஃ) $\frac{7}{-18}<\frac{-5}{12}<\frac{4}{-9}<\frac{-2}{3}$
(అ) $\frac{4}{-9}<\frac{7}{-18}<\frac{-5}{12}<\frac{-2}{3}$
(ङ) $\frac{-2}{3}<\frac{-5}{12}<\frac{4}{-9}<\frac{7}{-18}$

(0) $\frac{-1}{2}$
(ஃ) 0
(అ) $\frac{12}{15}$
(ఆ) ఓఏోిజ ๔్జి ణు,జజు

(o) $\frac{18}{1000}$
(\%) $\frac{18}{990}$
(అ) $\frac{18}{9900}$
(अ) $\frac{18}{999}$


$$
\frac{5}{1+\frac{1}{3+\frac{1}{2 \frac{1}{4}}}}
$$

(0) $\frac{40}{31}$
(ஃ) $\frac{4}{9}$
(అ) $\frac{1}{8}$
(अ) $\frac{31}{40}$

(०) $\square \frac{1}{4}$
(ஃ) $\square \frac{3}{20}$
(అ) $\square \frac{3}{10}$
(ఆ) $\square \frac{7}{20}$

(o) $\frac{2}{3}, \frac{3}{5}, \frac{7}{9}, \frac{9}{11}, \frac{8}{9}$
(ஃ) $\frac{3}{5}, \frac{2}{3}, \frac{9}{11}, \frac{7}{9}, \frac{8}{9}$
(అ) $\frac{3}{5}, \frac{2}{3}, \frac{7}{9}, \frac{9}{11}, \frac{8}{9}$
(ఆ) $\frac{8}{9}, \frac{9}{11}, \frac{7}{9}, \frac{2}{3}, \frac{3}{5}$

(o) $\frac{1}{4}$
(ஃ) $\frac{23}{24}$
(అ) $\frac{11}{12}$
(ङ) $\frac{17}{24}$
11. $5 \square\left[\frac{3}{4}+\left\{2 \frac{1}{2}-\left(0.5+\overline{\frac{1}{6}-\frac{1}{7}}\right)\right\}\right]:-$
(o) $2 \frac{23}{84}$
(ะ) $3 \frac{1}{6}$
(అ) $3 \frac{3}{10}$
(अ) $5 \frac{1}{10}$
12. ญజి $2805 \div 2.55=1100$, ణuజీక $280.5 \div 25.5=$
(0) 1.1
(ஃ) 1.01
(అ) 0.11
(ఆ) 11
13. ఇख్టటఙిణజ: $\frac{8-[5-(-3+2)] \div 2}{|5-3|-|5-8| \div 3}$
(o) 2
(ஃ) 3
(అ) 4
(ఆ) 5

[ఓవిఱఱ-2008]
(0) $\frac{4}{10}$
(ஃ) $\frac{4}{9}$
(అ) $\frac{4}{100}$
(अ) $\frac{9}{4}$

(o) 81
(ะ) 24
(అ) 192
(ఆ) 375
16. ఖชజి 甲 <2, ణబుజబటి 11

[ఓవిఖణ-2008]
(0) $2+\Phi$
(ஃ) $甲$
(అ) $\square \Phi$
(ఆ) $\square(2+\Phi)$

(0) $\frac{7}{162}$
(\%) $\frac{162}{7}$
(అ) $\frac{163}{7}$
(ङ) $\frac{7}{163}$


(ஃ) Oటతఒఒథి టజ ణ્,జిట 1
(అ) 0టతిజిథి జడ్జియిట ణఠ 1


(o) $\frac{1}{n}$
(ஃ) $\frac{2}{n}$
(అ) $\frac{2(\mathrm{n}-1)}{\mathrm{n}}$
(ఆ) $\frac{2}{\mathrm{n}(\mathrm{n}+1)}$

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20．2ీజ జీట $\mathfrak{a z ~ జ ి ~}\left(\frac{x^{b}}{x^{c}}\right)^{\frac{1}{b c}} \times\left(\frac{x^{c}}{x^{a}}\right)^{\frac{1}{c a}} \times\left(\frac{x^{a}}{x^{b}}\right)^{\frac{1}{a b}} \rho:$
（0）$甲$
（ஃ）$\frac{1}{x}$
（అ）$\square 1$
（ఆ） 1

（o） 0
（8）$\varnothing^{3+\varphi+\varphi+\varphi}$
（అ）$\frac{1}{\mathrm{x}^{\mathrm{a}+\mathrm{b}+\mathrm{c}}}$
（ఆ） 1

22．$\left(\frac{\mathrm{a}^{-1} \mathrm{~b}^{-1}}{\mathrm{a}^{-1}+\mathrm{b}^{-1}}-\frac{\mathrm{a}^{-1} \mathrm{~b}^{-1}}{\mathrm{a}^{-1}-\mathrm{b}^{-1}}\right)$ स्ञाओ ణo：
（0）$\frac{2 b}{b^{2}-a^{2}}$
（ஃ）$\frac{2 b}{a^{2}-b^{2}}$
（అ）$\frac{2 \mathrm{a}}{\mathrm{b}^{2}-\mathrm{a}^{2}}$
（ఆ）$\frac{2 a}{a^{2}-b^{2}}$




（ఆ）ఓबటిజ ๔ి ణు，జజ

24． $2.2 \overline{34}=$
（0）$\frac{1101}{495}$
（ะ）$\frac{1103}{495}$
（అ）$\frac{1106}{495}$
（ఆ）$\frac{1105}{495}$

（o）$\sqrt{19}$
（ஃ）$\sqrt{16}$
（అ）$\sqrt{17}$
（अ）$\sqrt{18}$

（0）$\frac{27161}{9999}$
（ஃ）$\frac{27}{99}$
（అ）$\frac{27161}{9900}$
（ఆ）$\frac{27161}{9000}$

27．2ి，జ 飞టట్జ ๔్జ $0.4 \overline{23} \mathrm{p}:$
（0）$\frac{423}{1000}$
（ஃ）$\frac{419}{1000}$
（అ）$\frac{423}{9000}$
（ङ）$\frac{419}{990}$

28．มృజి $\Phi=3+\sqrt{8}$ జటటిజ $甲=3 \square \sqrt{8}$ ణజజీ $\frac{1}{\mathrm{x}^{2}}+\frac{1}{\mathrm{y}^{2}}=$
（0）$\square 34$
（8） 34
（అ） $12 \sqrt{8}$
（丹）$\square 12 \sqrt{8}$

29． $1+\frac{1}{1+\frac{1}{1+\frac{1}{3}}}$, జడ్విట్ ణo $\square$
（0）$\frac{1}{3}$
（\％）$\frac{11}{7}$
（అ） 3
（अ） $1 \frac{1}{3}$

30 ．$\frac{\left(x^{a+b}\right)^{2}\left(x^{b+c}\right)^{2}\left(x^{c+a}\right)^{2}}{\left(x^{a} \times x^{b} \times x^{c}\right)^{4}}=$ ？
（0）$\square$
（ஃ） 0
（అ） 1
（ఆ）ఓఠటిజ ๔్జి ణ，జ్జు

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| Que． | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| Ans． | B | C | B | A | A | D | C | B | C | D | A | D | D | B | A |
| Que． | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| Ans． | D | A | C | B | D | D | D | A | C | B | C | D | B | B | C |

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