

|         | TRIGONOMETRIC EQUATIONS                                                                                                                                                                   |  |
|---------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--|
|         | PRINCIPAL SOLUTIONS:-                                                                                                                                                                     |  |
| Q.20)   | Find the principal solutions of $\csc x = -2$                                                                                                                                             |  |
| Sol.20) | $\Rightarrow \sin x = \frac{-1}{2}$                                                                                                                                                       |  |
|         | $3^{rd}$ quadrant, $\sin x = \sin \left(\pi + \frac{\pi}{6}\right)$                                                                                                                       |  |
|         | $\Rightarrow \sin x = \sin\left(\frac{7\pi}{6}\right)$                                                                                                                                    |  |
|         | 4 <sup>th</sup> quadrant, $\sin x = \sin \left(2\pi + \frac{\pi}{6}\right)$                                                                                                               |  |
|         | $\Rightarrow \sin x = \sin\left(\frac{11\pi}{6}\right)$                                                                                                                                   |  |
|         | $\Rightarrow x = \frac{7\pi}{6}$ and $x = \frac{11\pi}{6}$ are the principal solutions                                                                                                    |  |
| Q.21)   | Find the principal solutions of $\csc x = -2$                                                                                                                                             |  |
| Sol.21) | cosec x                                                                                                                                                                                   |  |
|         | $\Rightarrow \sin x = \frac{-1}{2}$                                                                                                                                                       |  |
|         | $3^{rd}$ quadrant $\sin y - \sin \left( \pi + \frac{\pi}{r} \right)$                                                                                                                      |  |
|         | $\Rightarrow \sin x = \sin\left(\frac{7\pi}{6}\right)$                                                                                                                                    |  |
|         | $\Rightarrow \sin x = \sin\left(\frac{7\pi}{6}\right)$ $4^{th} \text{ quadrant, } \sin x = \sin\left(2\pi + \frac{\pi}{6}\right)$ $\Rightarrow \sin x = \sin\left(\frac{11\pi}{6}\right)$ |  |
|         | $-3 \sin \lambda = \sin \left(\frac{1}{6}\right)$                                                                                                                                         |  |
|         | $\Rightarrow x = \frac{7\pi}{6}$ and $x = \frac{11\pi}{6}$ are the principal solutions                                                                                                    |  |
| Q.22)   | Find the principal solutions of $\tan x = \sqrt{3}$                                                                                                                                       |  |
| Sol.22) | $\tan x = \sqrt{3}$                                                                                                                                                                       |  |
|         | $1^{\rm st}  {\rm quadrant},  {\rm tan}  x = {\rm tan} \left( \frac{\pi}{3} \right)$                                                                                                      |  |
|         | $\Rightarrow x = \frac{\pi}{3}$                                                                                                                                                           |  |
|         | $3^{rd}$ quadrant, $\tan x = \tan \left(\pi + \frac{\pi}{3}\right)$                                                                                                                       |  |
|         | $\Rightarrow \tan x = \tan\left(\frac{4\pi}{3}\right)$                                                                                                                                    |  |
| 0.00)   | $\therefore x = \frac{\pi}{3} \text{ and } x = \frac{4\pi}{3} \text{ are the principal solutions}$                                                                                        |  |
| Q.23)   | Find the principal solutions of, $\sec x = -1$                                                                                                                                            |  |
| Sol.23) | $ \sec x = -1 \\ \Rightarrow \cos x = -1 $                                                                                                                                                |  |
|         | $2^{\text{nd}} \text{ quadrant, } \cos x = \cos(\pi - 0)$                                                                                                                                 |  |
|         | $\Rightarrow x = \pi$                                                                                                                                                                     |  |
|         | $3^{rd}$ quadrant, $\cos x = \cos(\pi + 0)$                                                                                                                                               |  |
|         | $\Rightarrow x = \pi$                                                                                                                                                                     |  |
|         | $\therefore x = \pi$ is the principal solutions                                                                                                                                           |  |