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Chapter 9

SEQUENCES AND SERIES

Arithmetic progression (A.P)

a, a+d, a+2d.....a+(n-1)d Standard AP $A_n = a + (n-1) d$ $S_n = \frac{n}{2}(2a + (n-1)d)$ $=\frac{n}{2}(a + an)$ Arithmetic mean A between the two numbers a and b is $\frac{a+b}{2}$ A = If A_1, A_2, \dots, A_n are n A.M between the two numbers a and b, $d = \frac{b-a}{n+1}$ Then $A_{1=} a + d = a + \frac{b-a}{n+1}$ $A_{2=} a + 2d = a + 2\frac{b-a}{n+1}$ $A_{n=} a + nd = a + n\frac{b-a}{n+1}$ Geometric progression (G.P) Standard GP \rightarrow a, ar, ar².....arⁿ⁻¹ $A_n = ar^{n-1}$ $a(r^n - 1)$ S 1

$$S_n = \frac{a(r-1)}{r-1} \text{ or } \frac{a(1-r)}{1-r} \quad \text{if } r \neq S_\infty = \frac{a}{1-r} \quad \text{if } |r| < 1$$

If G is the GM between a and b, then $G = \sqrt{ab}$

If $G_{1,}G_{2,\ldots,}G_{n}$ are n G.M between the two numbers a and b,

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then $r = \left(\frac{b}{a}\right)^{\frac{1}{n+1}}$ $G_1 = ar = a \left(\frac{b}{a}\right)^{\frac{1}{n+1}}$ $G_2 = ar^2 = a \left(\frac{b}{a}\right)^{\frac{2}{n+1}}$ Downloaded from www.studiestoday.com

$$G_n = ar^n = a\left(\frac{b}{a}\right)^{\frac{n}{n+1}}$$

Sum to n terms of special series

$$S_{n} = 1 + 2 + 3 + \dots + n = \frac{n(n+1)}{2}$$

$$S_{n} = 1^{2} + 2^{2} + 3^{2} + \dots + n^{2} = \frac{n(n+1)(2n+1)}{6}$$

$$S_{n} = 1^{3} + 2^{3} + 3^{3} + \dots + n^{3} = \frac{\{n(n+1)\}^{2}}{4}$$

TEXT BOOK QUESTIONS

- * \rightarrow Exercise 9.2 \rightarrow Qns 5,7,8,11,14
- * \rightarrow Exercise 9.3 \rightarrow Qns 2,3,5,11,16,17,19,21,23,25
- * \rightarrow Exercise 9.4 \rightarrow Qns 3,4,5,6,7
- * \rightarrow Misc Exercise \rightarrow Qns 3,4,5,10,12,14,18,21
- ** \rightarrow Exercise 9.2 \rightarrow Qns 9,10,12,13,15
- ** \rightarrow Exercise 9.3 \rightarrow Qns 12,13,14,15,18,22,26,27,28
- ** \rightarrow Exercise 9.4 \rightarrow Qns 1,2,8,9,10
- ** \rightarrow Misc Exercise \rightarrow Qns 19,22,23,24, 25,26
- ** \rightarrow Examples 4,5,6,10,13,18,21

EXTRA/ HOT QUESTIONS

1. Which term of the sequence 25, $24\frac{1}{4}$, $23\frac{1}{2}$, $22\frac{3}{4}$,....is the first negative term. (Ans.35)

2. How many terms are identical in the two AP.

2,4,6,..... up to 100 terms and 3,6,9..... up to 80 terms (Ans.33)

3. solve for x : 1+4+7+...+x = 590 (Ans.x=58)

4. Find the sum of all the three digit numbers which leaves the reminder 2 when divided by 5. (Ans.98910) Downloaded from www.studiestoday.com

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5. The digits of a three digit natural number are in AP and their sum is15. The number obtained by reversing the digits is 396 less than the original number. Find the number.

- 6. If pth, qth, and rth terms of GP are in GP. Show that p,q,r are in AP
- 7. If a,b,c,d are in GP, then show that $a^2 + b^2$, $b^2 + c^2$, $c^2 + d^2$ are in GP
- 8. Evaluate $7^{\frac{1}{2}} \times 7^{\frac{1}{4}} \times 7^{\frac{1}{8}}$ to infinite terms.

9. The common ratio of a GP is (- 4/5) and sum to infinity is (80/9). Find the first term. (Ans.7)

10. If S_1, S_2, S_3 are the sums of first n, 2n, 3n terms of a GP. Then Show that $s_1 (s_3-s_2) = (s_2-s_1)^2$

11. $\frac{1}{x+y}$, $\frac{1}{y+z}$, $\frac{1}{x+z}$ are in AP Show that y^2 , x^2 and z^2 are in AP.

12. Find the sum of $10^3 + 11^3 + \dots + 20^3$

(Ans.42075)

13. Find the nth term and the sum of n terms of the series

 $\frac{1}{2.5}$ + $\frac{1}{5.8}$ + $\frac{1}{8.11}$ +

14. Find the sum of n terms of $1^3 + \frac{1^3 + 2^3}{2} + \frac{1^3 + 2^3 + 3^3}{3} + \dots$

15. If AM and GM of roots of a quadratic equation are 8 and 5 respectively, then write the quadratic equation. $(Ans.x^2-16x+25=0)$

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