

	SEQUENCE AND SERIES				
0.1)	Class XI				
Q.1)	The sum of <i>n</i> terms of two A.P.'S are in the ratio $(3n + 8)$: $(7n + 15)$. Find the ratio of the in 12 th terms				
Sol 1)					
501.1)					
	First torm: a	Z A.P.			
	Difference: d	Pifference: d1			
	12^{th} torm: a	1 oth terms of			
	Sum S	12° term: a_{12}			
	$\frac{3411.5_n}{a_{12}} = \frac{a_{12}}{a_{13}}$	Sum S n			
	To find: $\frac{a_{12}}{a_{12}^1}$ i.e., $\frac{a_{111}}{a_{1111}^1}$				
	Given: $\frac{S_n}{S_n} = \frac{3n+18}{5}$				
	$\frac{n}{n}[2a+(n-1)d] = 2n+9$				
	$\Rightarrow \frac{2^{[2n+(n-1)d^{1}]}}{n[2n^{1}+(n-1)d^{1}]} = \frac{3n+6}{7n+15}$				
	$\begin{bmatrix} 2^{2}(2a+(n-1)a) \end{bmatrix}$ $3n+8$				
	$\Rightarrow \frac{1}{[2a^1 + (n-1)d^1]} = \frac{1}{7n+15}$				
	Put $n = 23$ both the sides				
	$\Rightarrow \frac{2a+22d}{a+2a+2a} = \frac{69+8}{161+47}$				
	$2a^{1}+22a^{1}$ 161+15 2(a+11d) 77				
	$\Rightarrow \frac{1}{2(a^1 + 11d^1)} \equiv \frac{1}{176}$				
	$\Rightarrow \frac{a_{12}}{a_{12}^4} = \frac{7}{16}$				
	Hence, the required ratio is 7: 16 ans.				
Q.2)	The ratio of the sum of $m \& n$ terms of an A.P.'S is $m^2: n^2$ show that the ratio of the m^{th}				
	term and n^{th} terms is $(2m-1)$: $(2n-1)$.				
Sol.2)	To prove: $\frac{a_m}{a} = \frac{2m-1}{2m-1}$				
	$a_n 2n-1$ $S_m m^2$				
	Given: $\frac{m}{S_n} = \frac{1}{n^2}$				
	$\rightarrow \frac{m}{2}[2a+(m-1)d] - m^2$				
	$\Rightarrow \frac{\pi}{2} [2a^{1} + (n-1)d^{1}] = \frac{\pi}{n^{2}}$				
	$\Rightarrow \frac{2a + (m-1)d}{2a + (m-1)d} = \frac{m}{2m}$				
	2a+(n-1)d n 2am + (mm - m)d - 2am + (mm - m)d	d = 0			
	$\Rightarrow 2an + (nm - n)d = 2am + (nm - m).d = 0$				
	$\Rightarrow 2a(n-m) + d(nm-n-nm+m) = 0$ $\Rightarrow 2a(n-m) - d(n-m) = 0$				
	$\Rightarrow 2u(n-m) = u(n-m) = 0$ $\Rightarrow (n-m)[2a-d] = 0$				
	$\Rightarrow (n - n)[2n - n] = 0$ $\Rightarrow (2n - d) = 0$				
	$\Rightarrow d = 2a$				
	$a_m = a + (m-1)(2a)$				
	Now, $\frac{1}{a_n} - \frac{1}{a + (n-1)(2a)}$				
	$=\frac{a+(1+2m-2)}{a+(1+2m-2)}$				
	$\Rightarrow \frac{a_m}{2m} = \frac{2m-1}{2m-1} (\text{proved})$				
	$a_n = \frac{2n-1}{2n-1}$ (proved)				
Q.3)	If the sum of <i>n</i> terms of an A.P. is $pn + qn^2$.	Find the common difference.			
Sol.3)	We have, $S_n = pn + qn^2$.				
	Put $n = 1, S_1 = p + q$				
	$\Rightarrow a_1 = p + q \dots \{ \because S_1 = a_1 \}$				
	Put $n = 2, S_2 = 2p + 4q$				

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	$\Rightarrow a_1 + a_2 = 2p + 4q \dots \{: S_1 = a_1 + a_2\}$		
	$\Rightarrow p + q + a_2 = 2p + 4q$		
	$\Rightarrow a_2 = p + 3q$		
	Now, $u = u_2 - u_1$ - $(n + 3a) - (n + a)$		
	$\begin{array}{l} -(p+3q)-(p+q)\\ d=2q \text{ ans.} \end{array}$		
Q.4)	The interior angles of a polygon are in A.P. The smallest angle is 120° & he common		
	difference is 5° . Find the number of sides of the polygon.		
Sol.4)	Let $n \rightarrow \text{no. of sides in the polygon}$		
	Interior angles form an A.P. with $a = 120^{\circ}$, $d = 5^{\circ}$, no. of term $= n$		
	Then, $S_n = \frac{n}{2} [240 + (n-1)5]$		
	$=\frac{n}{2}[240+5n-5]$		
	$S_n = \frac{n}{2} [5n + 235]$ (i)		
	Also, sum of all interior angles in any polygon with n-sides = $(n - 2) \times 180^{\circ}$ (ii)		
	Equation (i) & (ii) r^{n}		
	$\Rightarrow \frac{-}{2}[5n+235] = (n-2) \times 180$		
	$\Rightarrow 5n^2 + 235n = (n-2) \times 180$		
	$\Rightarrow 5n^{2} + 235n = 360n - 720$ $\Rightarrow 5n^{2} + 125n + 720 = 0$		
	$\Rightarrow 5n + 125n + 720 = 0$ $\Rightarrow n^2 - 25n + 144 = 0$		
	$\Rightarrow (n-16)(n-9) = 0$		
	\Rightarrow <i>n</i> = 16 or <i>n</i> = 9		
	When $n = 16$,		
	Then, $a_{16} = a + 15d$		
	= 120 + 15(5) = 105 > 100° (net pescible winterior angle connet > 100°)		
	$= 195 > 180$ (not possible \div interior angle cannot > 180) When $n = 9$		
	Then, $a_0 = a + 8d$		
	= 120 + 8(5)		
	$= 160 < 180^{\circ}$ (possible)		
	\therefore no. of sides in the polygon= 9 ans.		
Q.5)	The sum of the first term p, q, r terms of an A.P. are a, b, c respectively. Show that		
	$\frac{a}{p}(q-r) + \frac{b}{q}(r-p) + \frac{c}{r}(p-q) = 0$		
Sol.5)	Let $A \rightarrow 1$ st term of A.P.		
	$D \rightarrow \text{common difference}$		
	Then $a_p = a = \frac{p}{2} [2A + (p-1)D]$		
	$(or)\frac{a}{2} = \frac{1}{2}[2A + (p-1)D]$		
	$\Rightarrow a_q = b = \frac{q}{2} [2A + (q - 1)D]$		
	$(or)\frac{b}{2} = \frac{1}{2}[2A + (q-1)D]$		
	And $a_r = c = \frac{r}{2} [2A + (r - 1)D]$		
	$(or)\frac{c}{2} = \frac{1}{2}[2A + (r-1)D]$		
	Now, taking L.H.S., $\frac{a}{p}(q-r) + \frac{b}{q}(r-p) + \frac{c}{r}(p-q)$		
	Putting value of $\frac{a}{p}$, $\frac{b}{q}$, $\frac{c}{r}$ from the above equations:		

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	$=\frac{1}{2}[2A + (p-1)D](q-r) + \frac{1}{2}[2A + (q-1)D](r-p) + \frac{1}{2}[2A + (r-1)D](p-q)$			
	$= \frac{1}{-\{2A(q-r) + (n-1)D(q-r) + 2A(r-p) + (q-1)D(r-p) + 2A(p-q)\}}$			
	$2 \frac{2(2n(q-r) + (p-1)D(q-r) + 2n(r-p) + (q-1)D(r-p) + 2n(p-q))}{(r-1)D(r-q)}$			
	$= \frac{1}{24(q-r)} + \frac{1}{(n-1)D(q-r)} + \frac{24(r-n)}{4(q-1)D(r-n)} + \frac{24(n-q)}{4(n-q)}$			
	$= \frac{1}{2} \left\{ 2A(q-r) + (p-1)D(q-r) + 2A(r-p) + (q-1)D(r-p) + 2A(p-q) + (m-1)D(m-q) \right\}$			
	$1_{(2)}$			
	$= \frac{1}{2} \{ 2A[q - r + r - p + p - q] + D[pq - r - q + r + rq - pq - r + p + rp - rq - p] $			
	+q			
	$=\frac{1}{2}[2A(0) + D(0)]$			
	$=\frac{1}{-}(0)$			
	= 0 R.H.S. ans.			
Q.6)	Insert 3 A.M.'S between 3 and 19.			
Sol.6)	Here, $a = 3, b = 19 \& n = 3$			
	Lt A.M.'S are $A_1, A_2, \& A_3$			
	Now, $d = \frac{1}{n+1} = \frac{1}{3+1} = \frac{1}{4} = 4$			
	$A_1 = a + a = 3 + 4 = 7$ $A_2 = a + 2d = 3 + 8 = 11$			
	$A_2 = a + 2a = 3 + 6 = 11$ $A_3 = a + 3d = 3 + 12 = 15$			
	∴ required no.s are 7,11,15 ans.			
Q.7)	For what value of $n, \frac{a^{n+1}+b^{n+1}}{a^n+b^n}$ is the A.M. between & b.			
Sol.7)	We have, $\frac{a^{n+1}+b^{n+1}}{a} = A.M.$			
	$\Rightarrow \frac{a^{n+1} + b^{n+1}}{a^n} = \frac{a + b}{a^n}$			
	$a^{n+b^{n}} = (a+b)(a^{n}+b^{n})$			
	$\Rightarrow 2a^{n+1} + 2b^{n+1} = a^{n+1} + ab^n + ba^n + b^{n+1}$			
	$\Rightarrow 2a^{n+1} - a^{n+1} + 2b^{n+1} - b^{n+1} = ab^n + ba^n$			
	$\Rightarrow a^{n+1} - b^{n+1} = ab^n + ba^n$ $\Rightarrow a^{n+1} - ba^n - ab^n - b^{n+1}$			
	$\Rightarrow a^{n} = ba^{n} = ab^{n} = b^{n}$ $\Rightarrow a^{n}(a-b) = b^{n}(a-b)$			
	$\Rightarrow a^n = b^n$			
	$\Rightarrow \frac{a^n}{b^n} = 1$			
	$\Rightarrow \left(\frac{a}{b}\right)^n = 1$			
	$\Rightarrow \left(\frac{a}{b}\right)^n = \left(\frac{a}{b}\right)^0$			
	$\Rightarrow n = 0$ ans.			
Q.8)	Between 1 and 31, m numbers are inserted so that resulting sequence is an A.P. if the			
Sol 9)	ratio of the 7" & $(m-1)^{m}$ number is 5:9. Find the value of m . We have $a = 1, b = 31, 8, n = m$			
301.6)	Now $d = \frac{b-a}{a}$			
	$d = \frac{31-1}{2} = \frac{30}{2}$			
	$\Rightarrow u = \frac{1}{m+1} = \frac{1}{m+1}$			
1	Given, $\frac{m_{\ell}}{m_{\ell}} = \frac{1}{2}$			

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	$\Rightarrow \frac{a+7d}{a+(m-1)d} = \frac{5}{9}$		
	$1+7\left(\frac{30}{m+1}\right) \qquad 5$		
	$\Rightarrow \frac{1}{a + (m-1)\left(\frac{30}{m+1}\right)} = \frac{1}{9}$		
	$\Rightarrow \frac{m+1+210}{m+1+20m+20} = \frac{5}{2}$		
	$\Rightarrow \frac{m+1+30m-30}{2} = \frac{5}{2}$		
	31m-19 = 9 $\Rightarrow 9m \pm 1899 = 155m = 145$		
	$\Rightarrow 5m + 1659 = 155m = 145$ $\Rightarrow 146m = 2044$		
	$\Rightarrow m = \frac{2044}{1000} = 14$		
	$\rightarrow m = \frac{1}{146} = 11$		
0 9)	$\rightarrow m - 14$ dis.		
Q.5)	If $a\left(\frac{-}{b}+\frac{-}{c}\right)$, $b\left(\frac{-}{c}+\frac{-}{a}\right)$, $c\left(\frac{-}{a}+\frac{-}{b}\right)$ are in A.P. show that a, b, c are also in A.P.		
Sol.9)	We have, $a\left(\frac{1}{b}+\frac{1}{c}\right)$, $b\left(\frac{1}{c}+\frac{1}{a}\right)$, $c\left(\frac{1}{a}+\frac{1}{b}\right)$ are in A.P.		
	Adding 1 in each term		
	$\Rightarrow a\left(\frac{1}{b}+\frac{1}{c}\right)+1, b\left(\frac{1}{c}+\frac{1}{a}\right)+1, c\left(\frac{1}{a}+\frac{1}{b}\right)+1$ are also in A.P.		
	$\Rightarrow a\left[\frac{1}{b}+\frac{1}{c}+\frac{1}{a}\right], b\left[\frac{1}{c}+\frac{1}{a}+\frac{1}{b}\right], c\left[\frac{1}{a}+\frac{1}{b}+\frac{1}{c}\right]$ are in A.P.		
	$\Rightarrow 2b\left[\frac{1}{c} + \frac{1}{a} + \frac{1}{b}\right] = a\left[\frac{1}{b} + \frac{1}{c} + \frac{1}{a}\right] + c\left[\frac{1}{a} + \frac{1}{b} + \frac{1}{c}\right]$		
	$\Rightarrow 2b\left[\frac{1}{a} + \frac{1}{b} + \frac{1}{c}\right] = \left(\frac{1}{a} + \frac{1}{b} + \frac{1}{c}\right)(a+c)$		
	$\Rightarrow 2b = a + c$		
	<i>a</i> , <i>b</i> , <i>c</i> are in A.P. (proved)		
Q.10)	Of the sum of three numbers in A.P. is 24 & their product is 440. Find the numbers.		
Sol.10)	Let the numbers are $a - d$, a , $a + d$		
	Sum = 24		
	$\therefore a - d + a + a + a + d = 24$ $\Rightarrow 2a - 24$		
	$\Rightarrow 3u = 24$ $\Rightarrow a = 8$		
	$\Rightarrow u = 0$ $\Rightarrow \text{Product} = 440$		
	$\Rightarrow (a-d)(a)(a+d) = 440$		
	Put $a = 8$		
	$\Rightarrow (8-d)(8)(8+d) = 440$		
	$\Rightarrow (8-d)(8+d) = \frac{440}{8} = 55$		
	$\Rightarrow 64 - d^2 = 55$		
	$\Rightarrow d^2 = 9$		
	$\Rightarrow d = 3 \& d = -3$		
	For $a = 8 \& a = 3$		
	NO.S are $11,0,5$		
L	•• required no.s are 5,8,11 (0r) 11,8,5	L	

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