

Class: XI

Subject : Mathematics

Assignment No. 2

1. Prove by the principle of Mathematical induction for all natural numbers:

$$\frac{1}{1.2} + \frac{1}{2.3} + \frac{1}{3.4} + \dots + \frac{1}{n(n+1)} = \frac{n}{n+1}$$

2. Prove by the principle of Mathematical induction for all natural numbers:

$$\sin \theta + \sin 2\theta + \sin 3\theta + \dots + \sin n\theta = \frac{\sin\left(\frac{n+1}{2}\theta\right) \sin \frac{n\theta}{2}}{\sin \frac{\theta}{2}}$$

3. Prove by the principle of Mathematical induction for all natural numbers:
 $(11^{n+2} + 12^{2n+1})$ is divisible by 133.

4. Find the conjugate of $\frac{(3+i\sqrt{5})(3-i\sqrt{5})}{(\sqrt{3}+i\sqrt{2})-(\sqrt{3}-i\sqrt{2})}$.

5. If $z = -5 + 2\sqrt{-4}$ then show that $z^2 + 10z + 41 = 0$ and hence evaluate $(z^4 + 9z^3 + 35z^2 - z + 4)$

6. Express the following complex number in polar form:

(i) $(\sqrt{3} + i)$

(ii) $\sin 60^\circ + i \cos 60^\circ$

(iii) $(1 - \cos \theta + i \sin \theta)$

(iv) $\frac{1+2i}{1-3i}$ (v) $(1+i\sqrt{3})$

7. Solve for x : $21x^2 - 28x + 10 = 0$.

8. Solve for x : $x^2 + 7ix + 6 = 0$.

9. Solve for x : $2x^2 - (3+7i)x - (3-9i) = 0$.

10. Solve: $\frac{3n+1}{3} - \frac{4x+5}{6} \leq \frac{4x+1}{6} - \frac{2x+3}{2}$.

11. A solution of 8% boric acid is to be diluted by adding a 2% boric acid solution to it. The resulting mixture is to be more than 4% but less than 6% boric acid. If we have 640 liters of the 8% solution, how many liters of the 2% solution will have to be added?

12. Find the region of the graph where all the inequalities $(x + 2y) \geq 0$, $(2x + y) \leq 4$, $x \geq 0$ and $y \leq 2$ hold good. Also find the ordered pairs of the vertices of the region.

13. Solve the system of linear inequations graphically:-
 $x + 2y \leq 8$, $2x + y \geq 2$, $x - y \leq 1$, $x \geq 0$, $y \geq 0$

14. Evaluate : (i) $\lim_{x \rightarrow \pi/4} \left(\frac{\operatorname{Cosec} x^2 - 2}{\cot x - 1} \right)$ (ii) $\lim_{x \rightarrow 0} \left(\frac{1 - \cos 5x}{1 - \cos 6x} \right)$

(iii) $\lim_{x \rightarrow 0} \left(\frac{\operatorname{Cosec} x - \cot x}{x} \right)$ (iv) $\lim_{x \rightarrow \pi/2} \left(\frac{\pi}{2} - x \right) \tan x$

15. Evaluate: (i) $\lim_{x \rightarrow 0} \left(\frac{\sqrt{1+x} - \sqrt{1-x}}{x} \right)$ (ii) $\lim_{x \rightarrow 0} \left(\frac{x}{\sqrt{1+x} - 1} \right)$ (iii) $\lim_{x \rightarrow 4} \frac{3 - \sqrt{5+x}}{(1 - \sqrt{5-x})}$

(iv) $\lim_{x \rightarrow a} \left(\frac{\sqrt{a+2x} - \sqrt{3x}}{\sqrt{3a+x} - 2\sqrt{x}} \right)$ (v) $\lim_{x \rightarrow a} \left(\frac{x\sqrt{x} - a\sqrt{a}}{x - a} \right)$ (vi) $\lim_{x \rightarrow 0} \left(\frac{(1+x)^6 - 1}{(1+x)^2 - 1} \right)$

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