

J.E.E. Main/ Advanced Foundation - XI Maths Worksheet

Time: 60 min

Chapter#2 : Relations & Functions

Full Marks:

- Q.1 Let $A = \{1,2\}$ and $B = \{3,4\}$. Write $A \times B$. How many subsets will $A \times B$ have? List them.
- Q.2 Let $A = \{1,2,3,\dots,14\}$. Define a relation R from A to A by $R = \{(x,y) : 3x-y = 0, \text{ where } x,y \in A\}$. Write down its domain, co-domain and range.
- Q.3 If $f(x) = x^2$, find $\frac{f(1.2) - f(1)}{1.2 - 1}$.
- Q.4 Find the inverse of the function of $x = \frac{3-5y}{2y-7}$.
- Q.5 If $n(A) = 3$ and $n(B) = 3$, then find $n(A \times B)$. (1 mark)
- Q.6 Let R be a relation from Q to Q defined by $R = \{(a,b) : a,b \in Q \text{ and } a-b \in \mathbb{Z}\}$. Show that
 (a) $(a,a) \in R$ for all $a \in Q$
 (b) $(a,b) \in R$ implies that $(b,a) \in R$
 (c) $(a,b) \in R$ and $(b,c) \in R$ implies that $(a,c) \in R$.
- Q.7 Let $A = \{9, 10, 11, 12, 13\}$ and let $f: A \rightarrow N$ be defined by $f(n) =$ the highest prime factor of n . Find the range of f . (3 marks)
- Q.8 Find the domain of the function $f(x) = \frac{x^2 + 2x + 1}{x^2 - 8x + 12}$.
- Q.9 Let $A = \{1, 2, 3, 4\}$ and $B = \{10, 12, 13, 14, 20\}$. Whether $f: A \rightarrow B$ defined by $f(1) = 10, f(2) = 12, f(3) = 13$ is a function? (1 mark)
- Q.10 Find the domain and the range of the real function f defined by $f(x) = |x - 1|$. (2 marks)
- Q.11 Examine the relation : $R = \{(2,1), (3,1), (4,1)\}$ and state whether it is a function or not?
- Q.12 A function f is defined by $f(x) = 3x - 4$. Write down the value of $f(5)$ and $f(-7)$.
- Q.13 Write the domain of the function $f(x) = \frac{x+1}{x^2+6x+5}$.
- Q.14 Let $A = \{1, 2, 6, 8\}$ and let R be a relation on A defined by $\{(a, b) : a, b \in A, b \text{ is exactly divisible by } a\}$ (2 marks)
 a) Write R in roster form.
 b) Find the domain of R .
 c) Find the range of R .
- Q.15 If f and g are two functions such that $f(x) = 5x + 2$ and $g(x) = x^2 + 3$, then find $f + g$ and $f - g$. (2 marks)
- Q.16 Write the domain of the function, $f(x) = \frac{x^2 - 2x + 3}{x^2 - x - 20}$.
- Q.17 A function f is defined by $f(x) = 2x - 5$. Write down the values of (2 marks)
 (i) $f(0)$, (ii) $f(7)$, (iii) $f(-3)$
- Q.18 If $f(x) = x^2 - \frac{1}{x^2}$, then find the value of : $f(x) + f\left(\frac{1}{x}\right)$.
- Q.19 Under which condition a relation f from A to B is said to be a function? (1 mark)
- Q.20 If $A = \{a_1, a_2\}$ and $B = \{b_1, b_2, b_3\}$, then write $A \times B$.