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CHAPTER - 4

PRINCIPLE OF MATHEMATICAL INDUCTION

KEY POINTS

- Induction and deduction are two basic processes of reasoning.
- Deduction is the application of a general case to a particular case. In contrast to deduction, induction is process of reasoning from particular to general.
- Principle of Mathematical Induction

Let P(n) be any statement involving natural number n such that

- (i) P(1) is true, and
- If P(k) is true implies that P(k + 1) is also true for some natural (ii) number k

then P(n) is true $\forall n \in N$

SHORT ANSWER TYPE QUESTIONS (4 MARKS)

Using the principle of mathematical induction prove the following for all $n \in N$:

1.
$$3.6 + 6.9 + 9.12 + \dots + 3n(3n + 3) = 3n(n + 1)(n + 2)$$

2.
$$\left(1-\frac{1}{2}\right)\left(1-\frac{1}{3}\right)\left(1-\frac{1}{4}\right) - - -\left(1-\frac{1}{n+1}\right) = \frac{1}{n+1}$$

- 3. $n^2 + n$ is an even natural number.
- 2^{3n} –1 is divisible by 7 4.
- 3²ⁿ when divided by 8 leaves the remainder 1. 5.

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- 6. $4^{n} + 15n 1$ is divisible by 9
- 7. $n^3 + (n + 1)^3 + (n + 2)^3$ is a multiple of 9.
- 8. $x^{2n-1} 1$ is divisible by $x 1, x \neq 1$
- 9. $3^n > n$
- 10. If x and y are any two distinct integers then $x^n y^n$ is divisible by (x y)
- 11. n < 2ⁿ
- 12. $a + (a + d) + (a + 2d) + \dots + [a + (n 1)d] = \frac{n}{2} [2a + (n 1)d]$
- 13. $3x + 6x + 9x + \dots$ to n terms $= \frac{3}{2}n(n+1)x$
- 14. 11ⁿ⁺² + 12²ⁿ⁺¹ is divisible by 133.

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