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CHAPTER 7

PERMUTATIONS (Arrangements) AND COMBINATIONS (selections)

In permutation **order is important**, since 27 & 72 are different numbers(arrangements). In combination order is not important.

• Fundamental principle of counting (FPC)

Station A		Station B		Station C
	m ways		n ways	

then by FPC there are mn ways to go from station A to station C

• The number of permutations of n different things taken r at a time, where repetition is not allowed is given by ${}^{n}P_{r} = n(n-1)(n-2).....(n-r+1)$ where $0 < r \le n$.

eg
$${}^{5}P_{2} = 5 \times 4 = 20$$

 ${}^{7}P_{3} = 7 \times 6 \times 5 = 210$

• Factorial notation: $n! = 1 \times 2 \times 3 \times \times n$, where n is a natural number

eg
$$5! = 1 \times 2 \times 3 \times 4 \times 5$$

we define $0! = 1$
also $n! = n(n-1)!$
 $= n(n-1)(n-2)!$

- ${}^{n}P_{r} = \underline{n!}$ Where $0 \le r \le n$ (n-r)!
- Number of permutations of n different things, taken r at a time, where repetition is allowed is **n**^r
- The number of combinations of n different things taken r at a time is given by

$$^{n}C_{r} = \underline{n(n-1)(n-2)....(n-r+1)}$$
, where 0< r≤n
1.2.3.....r
eg $^{5}C_{3} = \underline{5 \times 4 \times 3} = {^{5}C_{2}}$
1 x 2 x 3

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{}^{n}C_{r} = {}^{n}C_{n-r}
 eg {}^{5}C_{3} = {}^{5}C_{2}
 ^{7}C_{5} = ^{7}C_{2}
^{n}C_{r} = n!, where 0 \le r \le n.
         r!(n-r)!
 {}^{n}C_{r} = {}^{n}C_{s} implies r = s or n = r+s (eg 17*) 1 mark
{}^{n}C_{n} = {}^{n}C_{0} = 1
^{n}C_{1} = n
 eg^{5}C_{1} = 5
^{n}C_{r} + ^{n}C_{r-1} = ^{n+1}C_{r}
 Ex 7.1
 1, 2, 4
 Ex 7.2
 4*, 5* (1 mark)
 eg 8* (1 mark), eg 11*, 12**,13**,14**,16** (4 marks)
 Ex 7.3
 7*, 8*, 9**, 10**, 11**
 Theorm 6 to prove (4 marks)*
 eg 17* (1 mark) use direct formula n = 9+8 = 17 since {}^{n}C_{r} = {}^{n}C_{s} implies r
 = s \text{ or } n = r + s
 eg 19**
 Ex 7.4
 2**,3*,5*,6*,7**,8*,9*
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eg 21**, eg 23*(HOT), eg 24*

Misc Ex

1**,2**,3**,4*,5*,7**,10**,11**

EXTRA/HOT QUESTIONS

- 1) How many permutations can be made with letters of the word MATHEMATICS ? In how many of them vowels are together?
- 2) In how many ways can 9 examination papers be arranged so that the best and the worst papers are never together. (HOT)
- 3) How many numbers greater than 56000 can be formed by using the digits 4,5,6,7,8; no digit being repeated in any number.
- 4) Find the number of ways in which letters of the word ARRANGEMENT can be arranged so that the two A's and two R's do not occur together. (HOT)
- 5) If C(2n,3): C(n,3):: 11:1 find n.
- 6) If P(11,r) = P(12,r-1) find r.

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- 7) Five books, one each in Physics, Chemistry, Mathematics, English and Hindi are to be arranged on a shelf. In how many ways can this be done?
- 8) If ${}^{n}P_{r} = {}^{n}P_{r+1}$ and ${}^{n}C_{r} = {}^{n}C_{r-1}$ find the values of n and r.
- 9) A box contains five red balls and six black balls. In how many ways can six balls be selected so that there are at least two balls of each color.
- 10) A group consist of 4 girls and 7 boys in how many ways can a committee of five members be selected if the committee has i) no girl ii) atleast 1 boy and 1 girl iii) atlest 3 girls.

Note : atleast means ≥

Answers

- 1) 4989600, 120960
- 2) 282240 Hint (consider the best and the worst paper as one paper)
- 3) 90
- 4) 1678320
- 5) 6
- 6) 9
- 7) 120
- 8) n = 3, r = 2
- 9) 425
- 10) i) 21
 - ii) 441
 - iii) 91