



Q.47)	If $n_{p_r} = n_{p_{r+1}}$ and $n_{c_r} = n_{c_{r+1}}$ , find the value of n & r ?	
Sol.47)	<p>We have, <math>n_{p_r} = n_{p_{r+1}}</math></p> $\Rightarrow \frac{n!}{(n-r)!} = \frac{n!}{(n-r)!}$ $\Rightarrow \frac{1}{(n-r)(n-r-1)!} = \frac{1}{(n-r-1)!}$ $\Rightarrow n-r=1 \dots \dots \dots (1)$ <p>We have, <math>n_{c_r} = n_{c_{r+1}}</math></p> $\Rightarrow \frac{n!}{r!(n-r)!} = \frac{n!}{(r+1)!(n-r-1)!}$ $\Rightarrow \frac{1}{r!(n-r)(n-r-1)!} = \frac{1}{(r+1)r!(n-r-1)!}$ $\Rightarrow \frac{1}{n-r} = \frac{1}{r+1}$ $\Rightarrow n-r = r+1 \dots \dots \dots (2)$ <p>from (1) &amp; (2),</p> $r+1 = 1$ $\Rightarrow r = 0 \text{ \& } n = 1 \text{ ans.}$	
Q.48)	In an examination, a question paper consists of 12 qns. Divided in to 2 parts, part 1 & part 2 containing 5 & 7 questions respectively. A student is required to attempt 8 questions in all selecting at least 3 questions from each part. In how many ways can be a student select questions?	
Sol.48)		420
Q.49)	Determine the number of 5 card combination out of a dick of 52 cards. If there is exactly one all in each combination?	
Sol.49)		$4c_1 \times 48c_4$
Q.50)	How many different words can be formed with the letters of word MISSISSPPI? In how many of these words in which 4 l's do not came together?	
Sol.50)	HINT : 4 l's not together = total words – 4 l's together words	
	$= \frac{11!}{4!4!2!} - \frac{8!}{4!2!} = 33810 \text{ ans.}$	
Q.51)	If $n_{c_8} = n_{c_6}$ , find $n_{c_2}$ ?	
Sol.51)	<p>We have, <math>n_{c_8} = n_{c_6}</math></p> $\Rightarrow n = 8+6 \dots \dots \dots \{prop. if n_{c_x} = n_{c_y} \text{ then } x+y = n\}$ $\Rightarrow n = 14$ <p>now, <math>n_{c_2} = 14c_2 = \frac{14 \times 13}{2} = 91 \text{ ans.}</math></p>	
Q.52)	We wish to select 6 persons from 8, but if the person A is chosen, then B must be chosen. In how many ways can the selection be made?	
Sol.52)	<p>HINT: two cases :</p> <p>Case 1): <math>6c_4</math> &amp; Case 2): <math>7c_6</math></p>	22
Q.53)	How many words can be formed by taking 4 letters at a time from the letter of the word MURADABAD?	
Sol.53)		Same as Q.19.. 626
Q.54)	There are 13 players out of which 4 are bowlers, in how many ways a team of 11 be selected such that	
	<ol style="list-style-type: none"> <li>1. there is no restriction on selectors</li> <li>2. 1 particular player never chosen</li> </ol>	



	3. 1 particular player always be chosen 4. Must include at least 3 bowlers									
Sol.54)	(1) $13_{C_{11}}$ , (2) $12_{C_{11}}$ , (3) $12_{C_{10}}$ , (4) $9_{C_8} \times 4_{C_3} + 9_{C_7} \times 4_{C_4}$									
Q.55)	A committee of 7 has to be formed from 9 boys & 4 girls. In how many ways can this be done, when committee consists of: 1. Exactly 3 girls 2. At least 3 girls 3. At most 3 girls 4. None of them is a girl 5. Boys are in majority 6. At least 3 from each gender 7. 1 particular boy and 1 particular girl never chosen									
Sol.55)	1. $9_{C_4} \times 4_{C_3}$ 2. $9_{C_4} \times 4_{C_3} + 9_{C_3} \times 4_{C_4}$ 3. $(9_{C_4} \times 4_{C_3}) + (9_{C_5} \times 4_{C_2}) + (9_{C_6} \times 4_{C_1}) + (9_{C_7} \times 4_{C_0})$ 4. $9_{C_7}$ 5. $(9_{C_4} \times 4_{C_3}) + (9_{C_5} \times 4_{C_2}) + (9_{C_6} \times 4_{C_1}) + (9_{C_7} \times 4_{C_0})$ 6. $(9_{C_4} \times 4_{C_3}) + (9_{C_3} \times 4_{C_4})$ 7. $11_{C_7}$									
Q.56)	Find the no. of ways in which 5 boys and 5 girls be seated in a row so that: 1. No 2 girls may sit together 2. All the girls never together									
Sol.56)	(1) $5! \times 6!$ , (2) $10! - 5! \times 6!$ ans.									
Q.57)	A code word is to consist of 2 distinct English alphabets followed by 2 distinct numbers from 1 to 9. For example, (A23) is a code word. (i) how many such code words are there and (ii) how many of them & with an even integer?									
Sol.57)	(i) $26_{P_2} \times 9_{P_2} = 46800$ ans. (ii) $9_{C_8} \times 8 \times 4 = 20800$ ans.									
Q.58)	A box contains 2 white balls, 3 black balls & 4 red balls. The number of ways of drawing 3 balls from the box if at least 1 black ball is to be included in the draw?									
Sol.58)	64 (3) (6) <table border="1"><tr><td>Black</td><td>Non- black</td></tr><tr><td>1</td><td>2</td></tr><tr><td>2</td><td>1</td></tr><tr><td>3</td><td>0</td></tr></table>	Black	Non- black	1	2	2	1	3	0	
Black	Non- black									
1	2									
2	1									
3	0									
Q.59)	A committee of 6 is to be chosen from 10 men & 7 women so as to contain at least 3 men & at least 2 women. In how many different ways can this be done if two particular women refuse to serve on the same committee?									
Sol.59)	Men = 10, women = 7 Required = 6 (i) Total no. of committees containing at least 3 women & 2 men are given by $= (10_{C_3} \times 7_{C_3}) + (10_{C_4} \times 7_{C_2})$ $= 4200 + 4410 = 8610$ (ii) No. of committees in which 2 particular women sure on the same committee $= (10_{C_4} \times 2_{C_2}) + (10_{C_3} \times 2_{C_2} \times 5_{C_1})$ $= 210 + 600 = 810$									



	(iii) Required no. of committees in which 2 particular women d not came together = Total – together = $8610 - 810$ = 7800 ans.	
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