Chapter - 13

(Surface areas and Volumes)

Key Concepts

SN.	Name	Figure	Lateral/curved surface area	Total surface area TSA	Volume (V)	Symbols use for
1	Cuboid	1	$2(l+b) \times h$	2(lb+bh+hl)	lbh	l = length b = breadth h = height
2.	Cube		4s ²	6s ²	s ³	s = side
3.	Right circular cylinder	Fort.	2πrh	$2\pi r(h+r)$	$\pi r^2 h$	h = height r = radius of base
4.	Right circular cone	$l^2 = r^2 + h^2$	πrl	$\pi r(l+r)$	$\frac{1}{3}\pi r^2 h$	r = radius of base h = height l = slant height
5.	Sphere		$4\pi r^2$	$4\pi r^2$	$\frac{4}{3}\pi r^3$	r = OA = radius
6.	Hemi sphere Solid	0	$2\pi r^2$	$3\pi r^2$	$\frac{2}{3}\pi r^3$	r = OA = radius
7.	Hemi sphere hollow	\bigcirc	$2\pi r^2$	$2\pi r^2$	$\frac{2}{3}\pi r^3$	r = OA = radius

Section - A

Q.1	If surface areas of two spheres are in the ratio of 4: 9 then the ratio of their volumes is						
	(a) $\frac{16}{27}$	(b) $\frac{4}{27}$	(c) $\frac{8}{27}$	(d) $\frac{9}{27}$			
Q.2	The surface area of a cube whose edge is 11cm is						
	(a) 725cm ²	(b) 726cm ²	(c) 727cm ²	(d) 728cm ²			
Q.3	A match box measures 4cm X 2.5cm X 1.5cm. What will be the volume of a						
	packet containing 12 such boxes?						
	(a) 15cm ³	(b) 180cm ³	(c) 90cm ³	(d) 175cm ³			
Q.4	The curved surface area of a right circular cylinder of height 14cm is 88cm ² . Find						
	the diameter of the base of the cylinder.						
	(a) 1cm	(b) 2cm	(c) 3cm	(d) 4cm			
Q.5	The total surface area of a cone of radius $\frac{r}{2}$ and length $2l$ is						
	(a) $2\pi r(l+r)$	(b) π <i>r</i>	r(l+r)				
	(c) $\pi r \left(l + \frac{r}{4} \right)$	(b) πr	$-\left(l+\frac{r}{2}\right)$				
Q.6	The surface area of sphere of radius 10.5cm is						
	(a) 1386cm ² (b) 616cm ²						
	(c) 1390cm ²	(d) 10	0cm ²				
		Section	ı - B				
Q.7	Find the volume of a sphere whose surface area is 154cm ² .						
Q.8	A solid cylinder has a total surface area of 231cm ² . Its curved surface area is $\frac{2}{3}$ or						
	the total surface area. Find the volume of the cylinder.						
Q.9	The diameter of a	The diameter of a garden roller is 1.4m and it is 2m long. How much area will it					

cover in 5 revolutions? ($\pi = 22/7$)

- Q.10 Three metal cubes whose edge measure 3cm, 4cm and 5cm respectively are melted to form a single cube, find its edge.
- Q.11 The dimensions of a cubiod are in the ratio of 1 : 2 : 3 and its total surface area is 88m². Find the dimensions.

Section - C

- Q.12 A cuboidal oil tin is 30cm X 40cm X 50cm. Find the cost of the tin required for making 20 such tins if the cost of tin sheet is Rs. 20/m².
- Q.13 Find the lateral curved surface area of a cylindrical petrol storage tank that is 4.2m in diameter and 4.5m high. How much steel was actually used, if $\frac{1}{12}$ of steel actually used was wasted in making the closed tank.
- Q.14 The radius and height of a cone are in the ratio 4 : 3. The area of the base is 154cm². Find the area of the curved surface.
- Q.15 A sphere, cylinder and cone are of the same radius and same height. Find the ratio of their curved surfaces.
- Q.16 A hemispherical bowl of internal diameter 36cm contains a liquid. This liquid is to be filled in cylindrical bottles of radius 3cm and height 6cm. How many bottles are required to empty the bowl?
- Q.17 A hemisphere of lead of radius 8cm is cast into a right circular cone of base radius 6cm. Determine the height of the cone.

Section - D

- Q.18 A wooden toy is in the form of a cone surmounted on a hemisphere. The diameter of the base of the cone is 6cm and its height is 4cm. Find the cost of painting the toy at the rate of Rs. 5 per 1000cm².
- Q.19 Find the volume of the largest right circular cone that can be fitted in a cube whose edge is 14cm.

- Q.20 A cone of height 24cm and slant height 25cm has a curved surface area 550cm². Find its volume use $\pi = \frac{22}{7}$
- Q.21 The radius and height of a cone are 6cm and 8cm respectively. Find the curved surface area of the cone.
- Q.22 A well with 10m inside diameter is dug 14m deep. Earth taken out of it is spread all around to a width of 5m to form an embankment. Find the height of embankment.
- Q.23 A metallic sheet is of the rectangular shape with dimensions 48cm X 36cm. From each one of its corners, a square of 8cm is cutoff. An open box is made of the remaining sheet. Find the volume of the box.

self evaluation

- Q.24 Water in a canal, 30dm wide and 12dm deep is flowing with a velocity of 20km per hour. How much area will it irrigate in 30min. if 9cm of standing water is desired? (10dm = 1 meter)
- Q.25 Three cubes of each side 4cm are joining end to end. Find the surface area of resulting cuboid.
- Q.26 A hollow cylindrical pipe is 210cm long. Its outer and inner diameters are 10cm and 6cm respectively. Find the volume of the copper used in making the pipe.
- Q.27 A semi circular sheet of metal of diameter 28cm is bent into an open conical cup. Find the depth and capacity of cup.
- Q.28 If the radius of a sphere is doubled, what is the ratio of the volume of the first sphere to that of second sphere?

Answer

- Q.1 c Q.2 b Q.3 b Q.4 b
- Q.5 c Q.6 a
- Q.7 179.66cm²
- Q.8 269.5cm² Q.9 44m²
- Q.10 6cm Q.11 2, 4, 6 cm
- Q.12 Rs. 376 Q.13 59.4m², 95.04m²
- Q.14 192.5cm²
- Q.15 4:4: $\sqrt{5}$ Q.16 72
- Q.17 28.44 Q.18 Rs. 0.51
- Q.19 718.66cm³ Q.20 1232 cm²
- Q.21 $60\pi \text{cm}^2$ Q.22 4.66m
- Q.23 5120cm³ Q.24 4,00,000m²
- Q.25 224 cm² Q.26 10560cm³
- Q.27 12.12cm, 622.26cm³
- Q.28 1:8